TARGET MATHEMATICS by:- AGYAT GUPTA







Code No. Series AG-4

CLASS XII

TMG-D/79/89

- Please check that this question paper contains 3 printed pages.
- Code number given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
- Please check that this question paper contains 29 questions.

General Instructions: -

- **1.** All questions are compulsory.
- 2. The question paper consists of 29 questions divided into three sections A, B and C. Section A contains 10 questions of 1 marks each, Section B is of 12 questions of 4 marks each and Section C is of 7 questions of 6 marks each.
- **3.** Write the serial number of the question before attempting it.
- **4.** If you wish to answer any question already answered, cancel the previous answer.
- 5. In questions where internal choices is provided. You must attempt only one choice.

MATHEMATICS

Time Allowed: 3 hours

Maximum Marks: 100

PART – A

- **1.** If $\vec{a} = \hat{i} 2\hat{j} + 3\hat{k} \& \vec{b} = \hat{i} 3\hat{k}$, find $|\vec{b} \times 2\vec{a}|$.
- 2. Find the value of c and d if the plane 2x + 4y cz + d = 0 will contain the line $\frac{x-1}{2} = \frac{y-3}{1} = \frac{z-1}{4}$.
- **3.** Evaluate: $\int_{-\pi/2}^{\pi/2} \log \left(\frac{2 \sin x}{2 + \sin x} \right) dx$.
- **4.** If $|\vec{a}| = \sqrt{26}$, $|\vec{b}| = 7 \& |\vec{a} \times \vec{b}| = 35$, find $\vec{a} \cdot \vec{b}$.
- **5.** Give an example of two non zero 2×2 matrix A,B such that AB = 0.
- **6.** Let $f: R \{-\frac{3}{5}\} \to R$ be a function as $f(x) = \frac{2x}{5x+3}$, Find f^{-1} .
- 7. If A, B, C are three non zero square matrix of same order, find the condition on A such that $AB = AC \Rightarrow B = C$.
- **8.** Find the values of λ for which the homogeneous system of 2x+3y-2z=0

equations: 2x - y + 3z = 0 find non – trivial solutions.

$$7x + \lambda y - z = 0$$

9. If the probability that a man aged 60 will live to be 70 is 0.4, what is the prob. that out of 3 men now 60, at least 2 will live to be 70?

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10. Find the coordinates of the point on the curve $y = x^2 - 6x + 9$ where the normal is parallel to the line y = x + 5.

- **11.**Prove that : $\tan \left[\frac{1}{2} \sin^{-1} \frac{2x}{1+x^2} + \frac{1}{2} \cos^{-1} \frac{1-y^2}{1+y^2} \right] = \frac{x+y}{1-xy}$.
- **12.** Evaluate : $\int \frac{2 \sin 2\phi \cos \phi}{6 \cos^2 \phi 4 \sin \phi} d\phi$.
- 13. Let T be the set of all triangles in a plane with R as a relation in T given by $R = \{(T_1, T_2): T_1 \sim T_2\}$. Show that R is an equivalence relation. Consider three right angle triangles T_1 with sides 3, 4, 5, T_2 with sides 5, 12, 13 and T_3 with sides 6, 8, 10. Which triangles among T_1 , T_2 and T_3 are related?
- **14.** Prove that If $y = \cos(\cos x)$; Prove that $\frac{d^2y}{dx^2} \cot x \frac{dy}{dx} + y \sin^2 x = 0$.
- **15.**Given that $\cos \frac{x}{2} \cdot \cos \frac{x}{4} \cdot \cos \frac{x}{8} = \frac{\sin x}{x}$, prove that $\frac{1}{2^2} \sec^2 \frac{x}{2} + \frac{1}{2^4} \sec^2 \frac{x}{4} + \dots = \cos ec^2 x \frac{1}{x^2}$.

If
$$x\sqrt{1+y} + y\sqrt{1+x} = 0$$
, prove that $\frac{dy}{dx} = -\frac{1}{(x+1)^2}$.

16. Given $\vec{a} = 3\hat{i} - \hat{j}$ and $\vec{b} = 2\hat{i} + \hat{j} - 3\hat{k}$, express \vec{b} as $\vec{b_1} + \vec{b_2}$ where $\vec{b_1}$ is parallel is $\vec{a} \& \vec{b_2}$ is perpendicular to \vec{a} .

If $\vec{a} = \hat{i} + 4\hat{j} + 2\hat{k}$, $\vec{b} = 3\hat{i} - 2\hat{j} + 7\hat{k}$ & $\vec{c} = 2\hat{i} - \hat{j} + 4\hat{k}$, find a vector \vec{d} which is perpendicular to both $\vec{a} \& \vec{b}$ and $\vec{c} . \vec{d} = 15$.

- 17. Using Lagrange's mean value theorem, find a point on the curve $y = \sqrt{x-2}$ defined on the interval [2, 3], where the tangent is parallel to the chord joining the end points of the curve.
- **18.**Evaluate: $\int \frac{\sqrt{x^2 + 1[\log(x^2 + 1) 2\log x]}}{4} dx$
- 19. The sum of the mean and variance of a Binomials distribution is 15 and the sum of their squares is 117. Determine the distribution
- 20. Show that $\begin{vmatrix} 2a & 3a + 2b & 4a + 3b + 2c \\ 3a & 6a + 3b & 10a + 6b + 3c \end{vmatrix} = a^3$. 21. Evaluate: $\int_{-1}^{3/2} |x \sin \pi x| dx$.

Evaluate
$$\int_{0}^{4} (|x-1| + |x-2| + |x-3|) dx$$
.

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22.In a particular city, 24% of the families earn less then Rs 3 lac annually, 70% earn less then Rs8 lac annually. The probability that a family owns a car is 10% if earning are below Rs 3 lac 55% if earning is between Rs3 lac and Rs8 lac, and 90 % if earning is above Rs8 lac. If we know that a family does have a car, what is the probability that its earning is between 3 lac and 8 lac

OR

Let X be the random variable which assumes values 0,1,2,3 such that 3P(X=0)=2P(X=1)=P(X=2)=4P(X=3). Find the probability distribution of X .Also find mean and variance .

PART - C

- **23.**If $A = \begin{bmatrix} 1 & -1 & 1 \\ 2 & 1 & -3 \\ 1 & 1 & 1 \end{bmatrix}$, find A^{-1} and hence solve the system of linear equations x + 2y + z = 4
 - x x + y + z = 0, x 3y + z = 2.

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24. A given quantity of metal is to be cast into a half cylinder with a rectangular base and semi-circular ends. Show that in order that the total surface area may be minimum, the ratio of the length of the cylinder to the diameter of its semi-circular ends is $\pi:(\pi+2)$.

OR

Show that the semi- vertical angle of a right circular cone of given surface area and maximum volume $is sin^{-1} \left(\frac{1}{3}\right)$.

25. Find the vector and Cartesian equation of the plane containing the two lines $\vec{r} = 2i + j - 3k + \lambda(i + 2j + 5k) \& \vec{r} = 2i + j - 3k + \mu(3i - 2j + 5k)$.

Also find the inclination of this plane with the XZ plane .

26.Sketch the graph $f(x) = \begin{cases} |x-2|+2 & x \le 2 \\ x^2-2 & x \ge 2 \end{cases}$. Evaluate $\int_0^4 f(x) dx$. What does this value represent on the graph?

OR

Find the area bounded by the curves $y = 6x - x^2 & y = x^2 - 2x$.

27. A housewife wishes to mix together two kinds of food $F_1 \& F_2$ in such a way that the mixture contains at least 10 units of vitamin A, 12 units of vitamin B and 8 units of vitamin C. The vitamin contents of one kg of foods $F_1 \& F_2$ are as below:

	VitaminA	VitaminB	VitaminC
$\operatorname{Food} F_1$	1	2	3
$\operatorname{Food} F_2$	2	2	1

One kg of food F_1 costs Rs 6 and one kg of food F_2 costs Rs 10. Formulate the above problem as a linear programming problem, and use iso – cost method to find the least cost of the mixture which will produce the diet.

- **28.** Prove that the image of the point (3, -2, 1) in the plane 3x y + 4z = 2 lies on the plane x + y + z + 4 = 0.
- **29.** Solve the initial value problems: $\sqrt{1-y^2} dx = (\sin^{-1} y x) dy$, y(0) = 0.

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