



Code No. **Series :AG-1-9999**

- Please check that this question paper contains 4 printed pages.
- Code number given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
- Please check that this question paper contains 30 questions.

General Instructions :-

1. Please check that this question paper contains 3 printed pages.
2. All questions are compulsory.
3. The question paper consists of 34 questions divided into four sections A, B and C & D .Section A contains 10 multiple choice type of questions of 1 marks each . Section B is of 8 questions of 2 marks each , Section C is of 10 questions of 3 marks each and Section D is of 6 questions of 4 marks each .
4. Write the serial number of the question before attempting it.
5. If you wish to answer any question already answered, cancel the previous answer.

Pre-Board Examination 2010 -11

Time: 3 hrs.

M.M.: 80

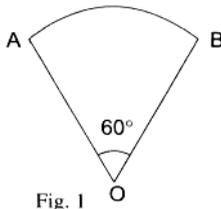
CLASS – X

MATHEMATICS

Section A

<p>Q.1</p>	<p>If one root of the equation $ax^2 + bx + c = 0$ is three times the other, then (a) $2b^2 = 9ac$ (b) $b^2 = 16ac$ (c) $b^2 = ac$ (d) $3b^2 = 16ac$. Ans d</p>
<p>Q.2</p>	<p>All Aces, Jacks and Queens are removed from a deck of playing cards. One card is drawn at random from the remaining cards. then the probability that the card drawn is not a face card. (A) 1/10 (B) 1/9 (C) $\frac{9}{10}$ (D) none Ans c</p>
<p>Q.3</p>	<p>Two tangents TP and TQ are drawn from an external point T to a circle with centre at O, as shown in Fig. 2. If they are inclined to each other at an angle of 100° then</p> <div style="text-align: center;"> <p>Fig. 2</p> </div> <p>what is the value of $\angle POQ$? (A) 60° (B) 110° (C) 100° (D) 80° Ans d</p>
<p>Q.4</p>	<p>If the numbers a, b, c, d, e form an AP , then the value of $a - 4b + 6c - 4d + e$ is (a) 1 (b) 2 (c) 0 (d) none of these Ans : c</p>
<p>Q.5</p>	<p>What is the distance between two parallel tangents of a circle of radius 4 cm? (A) 12 cm (B) 4 cm (C) 8 cm (D) none Ans c</p>
<p>Q.6</p>	<p>If Figure is a sector of a circle of radius 10.5 cm, find the perimeter of the sector.</p>

(Take $\pi = 22/7$)



(A) 32 cm (B) 11 cm (C) 66 cm (D) none **Ans a**

Q.7 If α, β are roots of the equation $x^2 + 5x + 5 = 0$, then equation whose roots are $\alpha + 1$ and $\beta + 1$ is
 (a) $x^2 + 5x - 5 = 0$ (b) $x^2 + 3x + 5 = 0$ (c) $x^2 + 3x + 1 = 0$ (d) none of these **Ans.c**

Q.8 The length of the tangent from a point A at a distance of 5 cm from the centre of the circle is 4 cm. What will be the radius of the circle?
 (A) 3 cm (B) 4 cm (C) 3 m (D) none **Ans a**

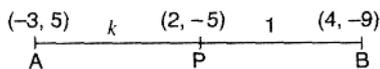
Q.9 The radii of the circular bases of frustum of a right circular cone are 12 cm and 3 cm and height is 12 cm. Find the total surface area
 (a) $378 \pi \text{ cm}^2$ (b) $2268 \pi \text{ cm}^2$ (c) 378 cm^2 (d) none of these **Ans.a**

Q.10 An electrician has to repair an electric fault on a pole of height 6 m. he needs to reach a point 2.54 m below the top of the pole. What should be the length of ladder that he should use which when inclined at an angle of 60° to the horizontal would enable him to reach the desired point? (take $\sqrt{3} = 1.73$)
 (a) 3.46 m (b) 4 m (c) 5.19 m (d) 7.5 m **Ans.b**

Section B

Q.11 In what ratio does the point P(2, -5) divide the line segment joining A(-3, 5) and B(4, -9)?

Sol.



Let AP : PB = k : 1

Coordinates of P = Coordinates of P

$$\left(\frac{4k-3}{k+1}, \frac{-9k+5}{k+1} \right) = (2, -5) \dots \text{(Using Section formula)}$$

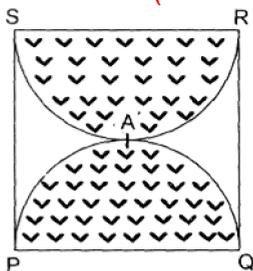
$$\therefore \frac{4k-3}{k+1} = \frac{2}{1}$$

$$\Rightarrow 4k - 3 = 2k + 2 \Rightarrow 4k - 2k = 2 + 3$$

$$\Rightarrow 2k = 5 \Rightarrow k = 5/2$$

$$\therefore \text{Required Ratio} = k : 1 = 5/2 : 1 = 5 : 2$$

Q.12 PQRS is a square land of side 28 m, Two semicircular grass covered portions are to be made on two of its opposite sides as shown in Figure 4. How much area will be left uncovered? (Take $\pi = 22/7$)



Sol. Area left uncovered
 = Area (square PQRS) - 2 Area (semicircle PAQ)
 $= (28 \times 28) \text{ m}^2 - 2 \left(\frac{\pi}{2} (14)^2 \right) \text{ m}^2$
 $= \left(784 - \frac{22}{7} \times 14 \times 14 \right) \text{ m}^2$ [\because Ar. of Square = (side)²
 Ar. of Circle = πr^2
 Side = 28 m
 Radius = $r = \frac{28}{2} = 14 \text{ m}$]
 $= (784 - 616) \text{ m}^2$
 $= \mathbf{168 \text{ m}^2}$

Q.13 Prove that the point (a, 0), (0, b) and (1, 1) are collinear if $\frac{1}{a} + \frac{1}{b} = 1$.

OR

Find a point on the y-axis which is equidistant from the points A(6,5) and B(-4, 3).

Sol. Let (0, y) be a point on the y-axis equidistant from A (6, 5) and B (-4, 3)

$$\Rightarrow PA = \sqrt{(6-0)^2 + (5-y)^2}$$

$$= \sqrt{y^2 - 10y + 61}$$

$$PB = \sqrt{(-4-0)^2 + (3-y)^2}$$

$$= \sqrt{y^2 - 6y + 25}$$

... [Using Distance formula]

Now, PA = PB
 $\Rightarrow (PA)^2 = (PB)^2$... (Squaring both sides)
 $\Rightarrow y^2 - 10y + 61 = y^2 - 6y + 25 \Rightarrow y^2 - 10y - y^2 + 6y = 25 - 61$
 $\Rightarrow -4y = -36 \Rightarrow y = 9$
 \therefore Required point is (0, 9)

Q.14 A bag contains 5 red balls, 8 green balls and 7 white balls. One ball is drawn at random from the bag. Find the probability of getting :

- (i) a white ball or a green ball.
- (ii) neither a green ball nor a red ball.

Sol. Total number of balls = 5 + 8 + 7 = 20

(i) P (white or green ball) = $\frac{15}{20} = \frac{3}{4}$
 (ii) P (neither green nor red) = $\frac{7}{20}$

Q.15 Find the area of the shaded region of Fig. 8, if the diameter of the circle with centre O is 28 cm and $AQ = \frac{1}{4}AB$.

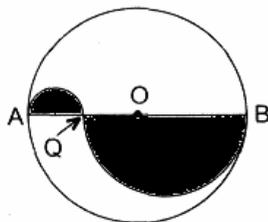


Fig. 8

Sol. Diameter AQ = $\frac{1}{4} \times 28 = 7 \text{ cm}$
 $\Rightarrow r = \frac{7}{2} \text{ cm}$
 Diameter QB = $\frac{3}{4} \times 28 = 21 \text{ cm}$
 $\Rightarrow R = \frac{21}{2} \text{ cm}$
 Area of shaded region = $\frac{1}{2} (\pi r^2 + \pi R^2)$
 $= \frac{\pi}{2} (r^2 + R^2)$
 $= \frac{1}{2} \cdot \pi \left[\left(\frac{7}{2} \right)^2 + \left(\frac{21}{2} \right)^2 \right]$

$$\begin{aligned}
 &= \frac{1}{2} \times \frac{22}{7} \times \left(\frac{49}{4} + \frac{441}{4} \right) \\
 &= \frac{1}{2} \times \frac{22}{7} \times \left(\frac{49+441}{4} \right) \\
 &= \frac{11}{7} \times \frac{490}{4} = \frac{770}{4} = 192.5 \text{ cm}^2.
 \end{aligned}$$

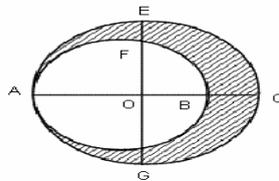
Q.16 A circle touches the side BC of a ΔABC at a point P and touches AB and AC when produced at Q and R respectively. Show that:
 $AQ = \frac{1}{2}$ (Perimeter of ΔABC).

Q.17 Solve for x : $\frac{x-1}{x-2} + \frac{x-3}{x-4} = 3\frac{1}{3}$ ($x \neq 2,4$). **Ans $x=5, \frac{5}{2}$**

Q.18 Determine an A.P. whose 3rd term is 16 and when 5th term is subtracted from the 7th term, we get 12.
Sol. Let the A.P. be **$a, a + d, a + 2d, \dots$**
 a is the first term and **d** is the common difference
 Using **$a_n = a + (n - 1)d$**
 A.T.Q. **$a + 2d = 16$ ($a_3 = 16$) ... (i)**
 $(a + 6d) - (a + 4d) = 12$ ($a_7 - a_5 = 12$) ... (ii) From (ii), **$a + 6d - a - 4d = 12$**
 $2d = 12 \Rightarrow d = 6$
 Putting the value of **d** in (i), we get
 $a = 16 - 2d \Rightarrow a = 16 - 2(6) = 4 \therefore$ Required A.P. = 4, 10, 16, 22,

Section C

Q.19 In the given figure, O is the centre of the bigger circle and AC is its diameter. Another circle with AB as diameter is drawn. If AC=54 cm and BC=10 cm, Find the area of the shaded region.



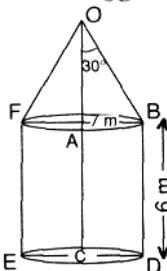
Ans 770cm

OR

The interior of a building is in the form of a right circular cylinder of radius 7 m and height 6m, surmounted by a right circular cone of same radius and of vertical angle 60° . Find the cost of painting the building from inside at the rate of Rs. 30/m².

Sol. Internal curved surface area of cylinder = $2\pi rh = (2\pi \times 7 \times 6)\text{m}^2$
 $= \left(2 \times \frac{22}{7} \times 7 \times 6 \right) \text{m}^2$
 $= 264 \text{ m}^2$ In right ΔOAB , $\frac{AB}{OB} = \sin 30^\circ$

Slant $\frac{7}{OB} = \frac{1}{2}$ height of cone (OB) = 14 m



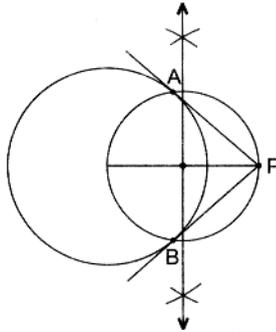
Internal curved surface area of cone = πrl

$$= \frac{22}{7} \times 7 \times 14 = 308\text{m}^2$$

Total area to be painted = $(264 + 308) = 572 \text{ m}^2$ Cost of painting @ Rs. 30 per $\text{m}^2 = \text{Rs. } (30 \times 572)$
 = Rs. 17,160

Q.20 Construct a circle whose radius is equal to 4 cm. Let P be a point whose distance from its centre is 6 cm. Construct two tangents to it from P.

Sol.



PA and PB are the required tangents.

Q.21 If the 10th term of an A.P. is 47 and its first term is 2, find the sum of its first 15 terms.

Sol. Let **a** be the first term and **d** be the common difference of an A.P.

$$a_{10} = 47, a = 2 \text{ (Given) } , \dots(i)$$

$$\Rightarrow a + 9d = 47 \text{ [}\because a_n = a + (n-1)d\text{]}$$

$$\Rightarrow 47 = 2 + (10 - 1)d \Rightarrow 47 = 2 + 9d \Rightarrow 9d = 47 - 2 = 45$$

$$\therefore d = \frac{45}{9} = 5$$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$\therefore S_{15} = \frac{15}{2} [2(2) + (15-1)(5)]$$

$$\Rightarrow S_{15} = \frac{15}{2} [4 + (14)(5)]$$

$$\Rightarrow S_{15} = \frac{15}{2} [4 + 70]$$

$$\Rightarrow S_{15} = \frac{15}{2} [74].$$

$$\therefore S_{15} = 15 (37) = 555$$

Q.22 The coordinates of the vertices of ΔABC are A (4,1), B (-3, 2) and C (0, **k**). Given that the area of ΔABC is 12 units², find the value of **k**.

Sol. ar (ΔABC) = 12 units² ...(Given)

$$\frac{1}{2} [4(2-k) + (-3)(k-1) + 0(1-2)] = 12 \text{ units}^2$$

$$[8-4k-3k+3] = \pm 24 \quad 11 - 7k = \pm 24 \quad -7k = \pm 24 - 11$$

$$k = \frac{\pm 24 - 11}{-7}$$

$$k = \frac{24 - 11}{-7}$$

$$k = \frac{+13}{-7}$$

$$\therefore k = \frac{-13}{7}$$

$$k = \frac{-24 - 11}{-7}$$

$$k = \frac{-35}{-7}$$

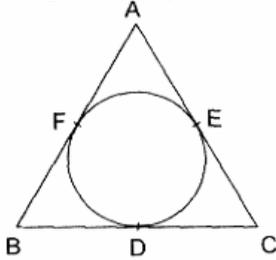
$$\therefore k = 5$$

Q.23 The product of two consecutive odd numbers is 483. find the numbers. **Ans.21,23**

Q.24 All Aces, Jacks and Queens are removed from a deck of playing cards. One card is drawn at random from the remaining cards. Find the probability that the card drawn is : **(a)** a face card **(b)** not a face card.

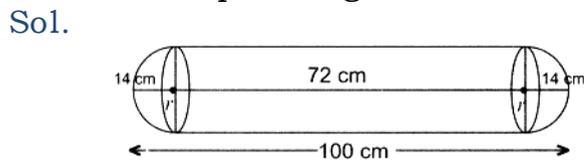
Sol. Total number of cards = 52
 Cards removed (all Aces, Jacks and Queens)
 = 12
 \therefore Remaining cards (Total) = 52 - 12 = 40
 Remaining face cards = 4 (all four kings)
 $P(\text{event}) = \frac{\text{Total number of favourable outcomes}}{\text{Total number of possible outcomes}}$
 $P(\text{getting a face card}) = \frac{4}{40} = \frac{1}{10}$
 $P(\text{not getting a face card}) = 1 - \frac{1}{10} \left[\begin{matrix} \therefore P(\text{not } A) \\ = 1 - P(A) \end{matrix} \right] = \frac{9}{10}$

Q.25 In Fig. 3 the incircle of $\triangle ABC$ touches the sides BC, CA and AB at D, E, and F respectively. If $AB = AC$, prove that $BD = CD$.



Sol. Given :
 The incircle of $\triangle ABC$ touches the sides BC, CA and AB at D, E and F respectively.
 $AB = AC$
 To prove : $BD = CD$
 Proof: Since the lengths of tangents drawn from an external point to a circle are equal
 \therefore We have $AF = AE$... (i)
 $BF = BD$... (ii)
 $CD = CE$... (iii)
 Adding (i), (ii) and (iii), we get
 $AF + BF + CD = AE + BD + CE$
 $\Rightarrow AB + CD = AC + BD$
 But $AB = AC$, ... (Given)
 $\therefore CD = BD$

Q.26 A solid is composed of a cylinder with hemispherical ends. If the whole length of the solid is 100 cm and the diameter of the hemispherical ends is 28 cm, find the cost of polishing the surface of the solid at the rate of 5 paise per sq cm.

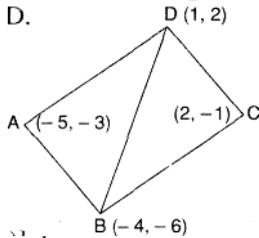


Radius of hemisphere, $r = 14$ cm
 Length of cylindrical part (h) = [100 - 2 (14)] = 72 cm
 Radius of cylindrical part
 = Radius of hemispherical ends, $r = 14$ cm
 Total area to be polished
 = 2 (C.S.A. of hemispherical end) + C.S.A. of cylinder
 $2 (2\pi r^2) + 2\pi r h = 2\pi r (2r + h)$

$$\begin{aligned}
 &= 2 \times \frac{22}{7} \times 14 (2 \times 14 + 72) \\
 &= 88 (28 + 72) = 8800 \text{ cm}^2 \text{ Cost of polishing the surface} \\
 &= 8800 \times 0.05 = \text{Rs. } 440
 \end{aligned}$$

Q.27 Find the area of the quadrilateral whose vertices taken in order are A (- 5, - 3), B (- 4, - 6), C (2, - 1) and D (1, 2).

Sol. Construction : Join B Proof : Area of quad. ABCD = Area of ΔABD + Area of ΔBCD Using area of Δ



$$\begin{aligned}
 &= \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)] \text{ ar}(\Delta ABD) \\
 &= \frac{1}{2} [-5(-6 - 2) - 4(2 + 3) + 1(-3 + 6)] \\
 &= \frac{1}{2} [-5(-8) - 4(5) + 1(3)] = \frac{1}{2} (40 - 20 + 3) \\
 &= \frac{1}{2} (23) = \frac{23}{2} \text{ units}^2 \text{ ar}(\Delta BCD) \\
 &= \frac{1}{2} [-4(-1 - 2) + 2(2 + 6) + 1(-6 + 1)] = \frac{1}{2} [4(-3) + 2(8) + 1(-5)] \\
 &= \frac{1}{2} (12 + 16 - 5) = \frac{1}{2} (23) = \frac{23}{2} \text{ units}^2 \\
 \therefore \text{ Area of quad. ABCD} &= \left(\frac{23}{2} + \frac{23}{2} \right) = 23 \text{ units}^2
 \end{aligned}$$

Q.28 A vertical tower stand on a horizontal plane and is surmounted by a vertical flagstaff of height h. at a point on the plane , the angle of elevation of the bottom of the flagstaff is α and that of the top of the flagstaff is β . Prove that the height of the tower is $\frac{h \tan \alpha}{\tan \beta - \tan \alpha}$.

Section D

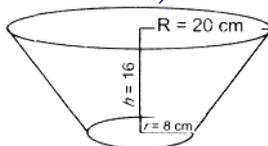
Q.29 A container (open at the top) made up of a metal sheet is in the form of a frustum of a cone of height 16 cm with radii of its lower and upper ends as 8 cm and 20 cm respectively. Find :

(i) the cost of milk when it is completely Filled with milk at the rate of Rs. 15 per litre.

(ii) the cost of metal sheet used, if it costs Rs. 5 per 100 cm^2 . (Take $\pi = 3.14$)

Sol. The container is in the shape of a frustum of a cone

$h = 16 \text{ cm}$, $r = 8 \text{ cm}$, $R = 20 \text{ cm}$



Volume of the container

$$\begin{aligned}
 &= \frac{1}{3} \times \pi h (R^2 + Rr + r^2) \\
 &= \frac{1}{3} \times 3.14 \times 16 [(20)^2 + 20(8) + (8)^2] \text{ cm}^3 \\
 &= \frac{1}{3} \times 3.14 \times 16 (400 + 160 + 64) \text{ cm}^3
 \end{aligned}$$

$$= \left(\frac{1}{3} \times 3.14 \times 16 \times 624\right) \text{cm}^3$$

$$= (3.14 \times 3328) \text{cm}^3$$

$$= 10449.92 \text{cm}^3 \quad \left[\begin{array}{l} 1 \text{ litre} = 1000 \text{ cm}^3 \\ 1 \text{ cm}^3 = \frac{1}{1000} \text{ lts} \end{array} \right]$$

$$= \frac{10449.92}{1000} \text{ litres}$$

$$= 10.45 \text{ litres (approx.) (i) Cost of milk} = 10.45 \times \text{Rs. } 15$$

$$= \text{Rs. } 156.75$$

Now, slant height of the frustum of cone

$$l = \sqrt{h^2 + (R - r)^2} = \sqrt{16^2 + (20 - 8)^2}$$

$$= \sqrt{256 + 144} = \sqrt{400} = 20 \text{ cm.}$$

Total surface area of the container

$$= [\pi l (R + r) + \pi r^2]$$

$$= [3.14 \times 20 (20 + 8) + 3.14 (8)^2] \text{ cm}^2$$

$$= 3.14 [20 \times 28 + 64] \text{ cm}^2$$

$$= 3.14 \times 624 \text{ cm}^2$$

$$= 1959.36 \text{ cm}^2$$

(ii) Cost of metal sheet used

$$= \text{Rs. } \left[1959.36 \times \frac{5}{100} \right] = \frac{9796.8}{100} = \text{Rs. } 97.968$$

$$= \text{Rs. } 98 \text{ (approx.)}$$

Q.30 From the top and foot of a tower 40 m high, the angle of elevation of the top of a lighthouse is found to be 30° and 60° respectively. Find the height of the lighthouse. Also find the distance of the top of the lighthouse from the foot of the tower.

Sol. Let AE = h m and BE = CD = x m

$$\therefore \frac{x}{h} = \cot 30^\circ$$

$$\Rightarrow \frac{x}{h} = \sqrt{3}$$

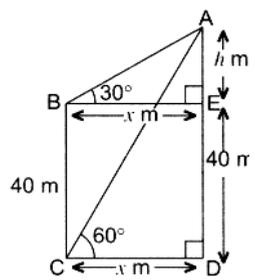
$$\Rightarrow x = h\sqrt{3} \quad \dots(i)$$

$$\Rightarrow BE = CD = h\sqrt{3} \text{ m}$$

In rt. ΔADC, $\frac{AD}{CD} = \tan 60^\circ$

$$\Rightarrow \frac{h + 40}{x} = \sqrt{3}$$

$$\Rightarrow h + 40 = \sqrt{3} x$$



$$\Rightarrow h + 40 = \sqrt{3} \times h\sqrt{3} \quad \dots [\text{From(i)}]$$

$$\Rightarrow 40 = 3h - h$$

$$\Rightarrow 2h = 40$$

$$\Rightarrow h = 20 \text{ m}$$

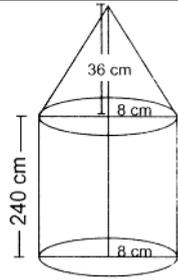
∴ Height of lighthouse = 20 + 40 = 60 m

In rt. ΔADC, $\frac{AD}{AC} = \sin 60^\circ$

$$\frac{60}{AC} = \frac{\sqrt{3}}{2} \Rightarrow \sqrt{3} AC = 60 \times 2$$

$$\Rightarrow AC = 60 \times 2 / \sqrt{3}$$

	$\Rightarrow AC = 60 \times \frac{2}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$ $\Rightarrow AC = \frac{60 \times 2 \times \sqrt{3}}{3} \Rightarrow AC = 40\sqrt{3}m$ <p>Hence the distance of the top of lighthouse from the foot of the tower = $40\sqrt{3}m$</p>
<p>Q.31</p>	<p>Prove that sum of n term of A . P . is $S_n = \frac{n}{2}[2a + (n - 1)d]$.</p> <p style="text-align: center;">OR</p> <p>A contract on construction job specifies a penalty for delay of completion beyond a certain date as follows : Rs. 200 for first day, Rs. 250 for second day, Rs. 300 for third day and so on.If the contractor pays Rs. 27,750 as penalty, find the number of days for which the construction work is delayed.</p> <p>Sol. Let the delay in construction work be for n days. Here $a = 200, d = 250 - 200 = 50, S_n = 27,750$ $S_n = \frac{n}{2}[2a + (n-1)d]$ $\therefore 27,750 = \frac{n}{2}[2 \times 200 + (n-1) 50]$ $27,750 = \frac{50n}{2} [8 + (n - 1)]$ $\frac{27,750}{25} = n(8 + n - 1)$ $1110 = n(n + 7) \Rightarrow 0 = n^2 + 7n - 1110$ $\Rightarrow n^2 + 7n - 1110 = 0$ $\Rightarrow n^2 + 31n - 30n - 1110 = 0$ $\Rightarrow n(n + 37) - 30(n + 37) = 0$ $\Rightarrow (n + 37) (n - 30) = 0$ $\Rightarrow n + 37 = 0$ or $n - 30 = 0$ Rejecting $n = - 37, n = 30$ (\therefore Number of days can not be negative) \therefore Construction work was delayed for 30 days</p>
<p>Q.32</p>	<p>If two tangents are drawn to a circle from an external point, then</p> <p>(i) They subtend equal angles at the centre.</p> <p>(ii) They are equally inclined to the segment, joining the centre to that point.</p>
<p>Q.33</p>	<p>Solve for x: $\frac{1}{a+b+x} = \frac{1}{a} + \frac{1}{b} + \frac{1}{x} : a \neq 0, b \neq 0, x \neq 0$. Ans = - a & - b</p> <p style="text-align: center;">OR</p> <p>A cottage industry produces a certain number of pottery articles in a day. It was observed on a particular day that the cost of production of each article was 3 more than twice the number of articles produced on that day. If the total cost of production on that day was Rs. 90 find the number of articles produced and the cost of each article. Ans. Articles 6,15</p>
<p>Q.34</p>	<p>An iron pillar has lower part in the form of a right circular cylinder and the upper part in the form of a right circular cone. The radius of the base of each of the cone and the cylinder is 8 cm. The cylindrical part is 240 cm high and the conical part is 36 cm high. Find the weight of the pillar if 1 cm³ of iron weighs 7.5 grams.</p> <p>(Take $\pi = \frac{22}{7}$)</p> <p>Sol. Radius of base of the cylinder, (r) = 8 cm Radius of base of the cone, (r) = 8 cm Height of cylinder, (h) = 240 cm Height of cone (H) = 36 cm</p>



Total volume of the pillar = Volume of cylinder + Volume of cone

$$= \pi r^2 h + \frac{1}{3} \pi r^2 H$$

$$= \pi r^2 \left(h + \frac{1}{3} H \right)$$

$$= \frac{22}{7} \times 8 \times 8 \left(240 + \frac{1}{3} (36) \right)$$

$$\frac{1408}{7} (240 + 12) \text{ cm}^3 \frac{1408}{7} \times 252 = 50688 \text{ cm}^3$$

$$\therefore \text{Weight of the pillar} = 50688 \times \frac{7.5(\text{gms.})}{1000} \text{ kg}$$

$$\frac{380160}{1000} = 380.16 \text{ kg}$$
