

CLASS – XI

MATHEMATICS

Section A

Q.1	Simplify : $\frac{\sin(180 + \theta) \cos(90 + \theta) \tan(270 - \theta) \cot(360 - \theta)}{\sin(360 - \theta) \cos(360 + \theta) \sec(-\theta) \sin(270 + \theta)}$. Ans : 1
Q.2	If A , B , C , D be the angles of a cyclic quadrilateral , taken in order , Prove that: $\cos(180-A) + \cos(180-B) + \cos(180+C) - \sin(90+D) = 0$.
Q.3	Prove that : $\cos 34^\circ + \cos 43^\circ + \cos 137^\circ + \cos 214^\circ + \cos 300^\circ = \frac{1}{2}$.
Q.4	Prove that : $2 \sin \frac{5\pi}{12} \sin \frac{\pi}{12} + 2 \cos \frac{5\pi}{12} \cos \frac{\pi}{12} = 1$.
Q.5	Prove that : $\cos(45^\circ - A)\cos(45^\circ - B) - \sin(45^\circ - A)\sin(45^\circ - B) = \sin(A+B)$.
Q.6	Evaluate: $\sec\left(\frac{3\pi}{2} - \theta\right)\sec\left(\theta - \frac{5\pi}{2}\right) + \tan\left(\frac{5\pi}{2} + \theta\right)\tan\left(\theta - \frac{3\pi}{2}\right)$. Ans - tan θ
Q.7	Evaluate: $\cot\left(\theta - \frac{75\pi}{2}\right)$. Ans - tan θ
Q.8	Find the value of $\tan\left(\frac{59\pi}{2} + \theta\right)$. Ans - cot θ
Q.9	Prove that $\tan 75^\circ - \tan 30^\circ - \tan 75^\circ \tan 30^\circ = 1$.
Q.10	$113\pi - \theta$ lies in which quadrant . Ans: 2nd Quadrant

Section B

Q.11	Prove that : $\sin 78^\circ \sin 48^\circ + \cos 120^\circ \sin 30^\circ = \frac{1}{2}$.
Q.12	Prove that : $\frac{\tan^2 2\theta - \tan^2 \theta}{1 - \tan^2 2\theta \tan^2 \theta} = \tan 3\theta \tan \theta$. OR Find the value of : $\sin 10^\circ + \sin 20^\circ + \sin 30^\circ + \dots + \sin 360^\circ$. Ans: 0
Q.13	If $\cos(\alpha + \beta) = \frac{7}{25}$, $\sin(\alpha - \beta) = \frac{8}{17}$ and α, β lie between 0 and $\frac{\pi}{4}$, find $\tan 2\alpha$ & $\tan 2\beta$. Ans $\tan 2\alpha = -\frac{416}{87}$ & $\tan 2\beta = \frac{364}{297}$ OR If $\tan x + \tan y = a$ and $\cot y + \cot x = b$, prove that $\frac{1}{a} - \frac{1}{b} = \cot(x+y)$.
Q.14	Prove that: $\tan 80^\circ - \tan 10^\circ = 2 \tan 70^\circ$. OR Prove that $\sqrt{3} \cos 23^\circ - \sin 23^\circ = 2 \sin 37^\circ$.
Q.15	Prove that : $\tan 7A - \tan 5A - \tan 2A = \tan 7A \tan 5A \tan 2A$.
Q.16	If $\tan \alpha = m/(m+1)$, $\tan \beta = 1/(2m+1)$ show that $\alpha + \beta = \frac{\pi}{4}$.
Q.17	Find x from the equation: $\operatorname{cosec}(90^\circ + \theta) - x \sin(90^\circ - \theta) \tan(180^\circ + \theta) = \sin(90^\circ + \theta)$. Ans $x = \tan \theta$
Q.18	Prove that $\cot \alpha \cot 2\alpha - \cot \alpha \cot 3\alpha - \cot 2\alpha \cot 3\alpha = 1$.
Q.19	Prove that : $\frac{\sin(A - B)}{\sin A \sin B} + \frac{\sin(B - C)}{\sin B \sin C} + \frac{\sin(C - A)}{\sin C \sin A} = 0$.

Q.20	Prove that $\sin 600^\circ \tan(-690^\circ) + \sec 840^\circ \cot(-945^\circ) = \frac{3}{2}$.
Q.21	Find the value of $\sin(\pi/12)$. Ans $\frac{\sqrt{3}-1}{2\sqrt{2}}$
Q.22	Prove that : $\cos \frac{2\pi}{3} \cos \frac{\pi}{4} - \sin \frac{2\pi}{3} \sin \frac{\pi}{4} = -\left(\frac{\sqrt{3}+1}{2\sqrt{2}}\right)$. OR If $\sin(\alpha + \beta) = 1$, $\sin(\alpha - \beta) = 1/2$; $\alpha, \beta \in [0, \pi/2]$, then find the value of $\tan(\alpha + 2\beta)$. Ans $-\sqrt{3}$
Section C	
Q.23	(i) Prove that : $\frac{\cos 17^\circ + \sin 17^\circ}{\cos 17^\circ - \sin 17^\circ} = \tan 62^\circ$. (ii) Prove that : $\frac{\operatorname{cosec}(90^\circ + \theta) + \cot(450^\circ + \theta)}{\operatorname{cosec}(90^\circ - \theta) + \tan(180^\circ - \theta)} + \frac{\tan(180^\circ + \theta) + \sec(180^\circ - \theta)}{\tan(360^\circ + \theta) - \sec(-\theta)} = 2$.
Q.24	If $A + B = 225^\circ$, prove that $\frac{\cot A}{1 + \cot A} \cdot \frac{\cot B}{1 + \cot B} = \frac{1}{2}$. OR If $\sin A = -\frac{5}{13}$, $\cos B = \frac{-3}{5}$, $270^\circ < A < 360^\circ$ and $180^\circ < B < 270^\circ$, find the values of $\tan(A + B)$ and $\sin(A - B)$. Ans $\tan(A + B) = 33/56$ & $\sin(A - B) = 63/65$
Q.25	If $\tan(\pi \cos \theta) = \cot(\pi \sin \theta)$ Prove that $\cos(\theta - \frac{\pi}{4}) = \pm \frac{1}{2\sqrt{2}}$. OR Prove that : (i) $\cos\left(\frac{\pi}{3} + x\right) = \frac{1}{2}(\cos x - \sqrt{3} \sin x)$ (ii) $\sin\left(\frac{\pi}{4} + x\right) + \sin\left(\frac{\pi}{4} - x\right) = \sqrt{2} \cos x$
Q.26	(i) If $A + B + C = 180^\circ$, prove that : $\tan A + \tan B + \tan C = \tan A \tan B \tan C$. (ii) If $A + B + C = 180^\circ$, prove that: $\cot \frac{A}{2} + \cot \frac{B}{2} + \cot \frac{C}{2} = \cot \frac{A}{2} \cot \frac{B}{2} \cot \frac{C}{2}$.
Q.27	(i) Simplify : $\frac{\tan(90^\circ + \theta) \sec(180^\circ + \theta) \sin(-\theta)}{\cot(180^\circ - \theta) \sin(360^\circ - \theta) \operatorname{cosec}(270^\circ + \theta)}$. Ans: 1 (ii) Simplify : $\frac{\tan(90^\circ - \theta) \sin(180^\circ + \theta) \sec(270^\circ + \theta)}{\cos(270^\circ - \theta) \operatorname{cosec}(180^\circ - \theta) \cot(360^\circ - \theta)}$. Ans: -1
Q.28	(i) If $\cos \alpha = 13/14$ & $\cos \beta = 1/7$ where α & β lies in Ist quadrant show that $\alpha - \beta = \frac{\pi}{3}$. (ii) If A lies in the second quadrant and $3 \tan A + 4 = 0$, then find the value of $2 \cot A - 5 \cos A + \sin A$. Ans $23/10$
Q.29	Find the value of (i) $\sin\left(\frac{31\pi}{3}\right)$ (ii) $\cos \frac{307\pi}{6}$ (iii) $\tan\left(-\frac{26\pi}{3}\right)$ (iv) $\cot(585^\circ)$ (v) $\operatorname{cosec}(-750^\circ)$ (vi) $\cos(-3750^\circ)$. Ans (i) $\frac{\sqrt{3}}{2}$ (ii) $-\frac{\sqrt{3}}{2}$ (iii) $\sqrt{3}$ (iv) 1 (v) -2 (vi) $-\frac{\sqrt{3}}{2}$
Think only of the best , work only for the best , and expect only the best	