



## CLASS XII

## DEFINITE INTEGRAL

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| <b>Q.1</b>  | Evaluate $\int_{-1}^1 (x - [x]) dx$ .  |
| <b>Q.2</b>  | Evaluate: $\int_0^{\pi/2} (2 \log \sin x - \log \sin 2x) dx$ .                               |
| <b>Q.3</b>  | Evaluate: $\int_{-\pi/2}^{\pi/2} \log\left(\frac{2 - \sin x}{2 + \sin x}\right) dx$ .        |
| <b>Q.4</b>  | If $f(a + b - x) = f(x)$ , prove that $\int_a^b xf(x) dx = \frac{a+b}{2} \int_a^b f(x) dx$ . |
| <b>Q.5</b>  | Evaluate: $\int_{-1}^1 x^{17} \cos^4 x dx$ .   |
| <b>Q.6</b>  | Write the value of $\int_{-\pi/2}^{\pi/2} \sin^5 x dx$ .                                     |
| <b>Q.7</b>  | Evaluate: $\int_0^{\pi/2} \log\left(\frac{4 + 3 \sin x}{4 + 3 \cos x}\right) dx$ .           |
| <b>Q.8</b>  | Evaluate $\int_0^{2\pi} \frac{dx}{1 + e^{\sin x}}$ .   |
| <b>Q.9</b>  | Evaluate: $\int_0^a \frac{1}{x + \sqrt{a^2 - x^2}} dx$ .                                     |
| <b>Q.10</b> | If $\int_0^k \frac{dx}{2+8x^2} = \frac{\pi}{16}$ . Find the value of k .                     |
| <b>Q.11</b> | Evaluate: $\int_0^2 x \sqrt{2-x} dx$ .   |

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| <b>Q.12</b> | Evaluate: $\int_{-\pi/2}^{\pi/2} \sin x  dx$ .   |
| <b>Q.13</b> | Evaluate: $\int_0^{\pi/4} \log(1 + \tan \theta) d\theta$ .                             |
| <b>Q.14</b> | Evaluate: $\int_{\pi/3}^{\pi/2} \frac{\sqrt{1 + \cos x}}{(1 - \cos x)^{3/2}} dx$ .     |
| <b>Q.15</b> | Evaluate $\int_0^2  x^2 + 2x - 3  dx$ .  |
| <b>Q.16</b> | Evaluate $\int_0^{1.5} [x^2] dx$ , where $[.]$ denotes the greatest integer function . |
| <b>Q.17</b> | Evaluate $\int_1^4 ( x-1  +  x-2  +  x-3 ) dx$ .                                       |
| <b>Q.18</b> | Evaluate $\int_1^2 (x^2 + x + 2) dx$ as a limits of sum .                              |
| <b>Q.19</b> | Evaluate: $\int_0^{\pi/2} \frac{\cos^2 x}{\cos^2 x + 4 \sin^2 x} dx$ .                 |
| <b>Q.20</b> | Evaluate: $\int_0^{\pi/2} \sin 2x \tan^{-1}(\sin x) dx$ .                              |
| <b>Q.21</b> | Evaluate: $\int_0^{\pi} \frac{x}{a^2 \cos^2 x + b^2 \sin^2 x} dx$ .                    |
| <b>Q.22</b> | Evaluate: $\int_{-1}^2  x \cos(\pi x)  dx$ .   |
| <b>Q.23</b> | Evaluate: $\int_0^a \sin^{-1} \sqrt{\frac{x}{a+x}} dx = \frac{a}{2} (\pi - 2)$ .       |
| <b>Q.24</b> | Evaluate: $\int_0^{\pi} x \log \sin x dx$ .  |

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| <b>Q.25</b> | Evaluate: $\int_0^1 \sin^{-1} \left( x\sqrt{1-x} - \sqrt{x}\sqrt{1-x^2} \right) dx$ . | <b>Q.39</b> | Evaluate : $\int_0^{\pi/2} (\sqrt{\tan x} + \sqrt{\cot x}) dx$ .  |
| <b>Q.26</b> | Evaluate : $\int_1^3 (5x^2 - e^x + 4) dx$ as a limit of sums                          | <b>Q.40</b> | Evaluate: $\int_{-\pi/4}^{\pi/4} \frac{x + \pi/4}{2 - \cos 2x} dx$ .  |
| <b>Q.27</b> | Evaluate: $\int_0^\pi \frac{x dx}{1 - \cos \alpha \sin x}$ .                          | <b>Q.41</b> | <b>Evaluate:</b> $\int_0^{\pi/4} \sqrt{\tan x} dx$  |
| <b>Q.28</b> | Evaluate : $\int_{-\pi}^{\pi} \frac{2x(1 + \sin x)}{1 + \cos^2 x} dx$ .               | <b>Q.42</b> | Evaluate: $\int_0^{2\pi} \frac{\sin 2x}{a - b \cos x} dx$ .   |
| <b>Q.29</b> | Evaluate $\int_0^\pi \frac{x dx}{(a^2 \cos^2 x + b^2 \sin^2 x)^2}$ .                  | <b>Q.43</b> | Evaluate: $\int_a^b \sqrt{\frac{x-a}{b-x}} dx$ .  |
| <b>Q.30</b> | Evaluate: $\int_{-a}^a \sqrt{\frac{a-x}{a+x}} dx$ .                                   | <b>Q.44</b> | Evaluate: $\int_0^{\pi/2} \sqrt{\tan x} dx$ .   |
| <b>Q.31</b> | Evaluate : $\int_1^3 (2x^2 + 3x + 7) dx$ as limit of sums.                            | <b>Q.45</b> | Evaluate: $\int_0^\pi \frac{x}{4 - \cos^2 x} dx$ .  |
| <b>Q.32</b> | If $\int_0^1 (3x^2 + 2x + k) dx = 0$ , find the value of k.                           | <b>Q.46</b> | Evaluate: $\int_0^\infty \frac{x}{(1+x)(1+x^2)} dx$ .   |
| <b>Q.33</b> | Evaluate: $\int_0^{3/2}  x \cos \pi x  dx$ .  | <b>Q.47</b> | Evaluate: $\int_1^5  x^2 - 5x + 6  dx$ .  |
| <b>Q.34</b> | Evaluate $\int_0^1 \frac{x}{x^2 + 1} dx$ .  | <b>Q.48</b> | If $f(x)$ is a continuous function defined on $[0, 2a]$ , then prove that<br>$\int_0^{2a} f(x) dx = \begin{cases} 2 \int_0^a f(x) dx, & \text{if } f(2a-x) = f(x) \\ 0, & \text{if } f(2a-x) = -f(x) \end{cases}$ |
| <b>Q.35</b> | Evaluate: $\int_0^{\pi} \frac{x}{a^2 - \cos^2 x} dx$ .                                | <b>Q.49</b> | Evaluate : $\int_0^{\pi/2} \frac{x}{\sin x + \cos x} dx$ .  |
| <b>Q.36</b> | Evaluate : $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$ .          | <b>Q.50</b> | If $f(x)$ is a continuous function defined on<br>$\int_{-a}^a f(x) dx = \begin{cases} 2 \int_0^a f(x) dx, & \text{if } f(-x) = f(x) \\ 0, & \text{if } f(-x) = -f(x) \end{cases}$                                 |
| <b>Q.37</b> | Find $\int_{-\pi}^{\pi} (\sin^{-93} x + x^{295}) dx$ .                                |             |   |
| <b>Q.38</b> | Evaluate: $\int_1^3 (5x^2 - e^{2x-5} + 4) dx$ , as limit of sums.                     |             |   |

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| <b>Q.51</b> | Evaluate $\int_{-1}^{\frac{3}{2}}  x \sin (\pi x)  dx$ .   |
| <b>Q.52</b> | Evaluate $\int_0^\pi \frac{e^{\cos x} dx}{e^{\cos x} + e^{-\cos x}}$ .                                 |
| <b>Q.53</b> | <b>Evaluate:</b> $\int_0^1 x(\tan^{-1} x)^2 dx$  |
| <b>Q.54</b> | Evaluate, $\int_0^1 [5x] dx$ (where $[x]$ is greatest integer function)                                |
| <b>Q.55</b> | Evaluate : $\int_0^{\pi/2} x \cot x dx$ .  |
| <b>Q.56</b> | Prove that : $\int_0^{\pi/2} \frac{\sqrt{\cos x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx = \frac{\pi}{4}$ . |
| <b>Q.57</b> | Evaluate: $\int_0^\pi \frac{x \tan x}{\sec x \cos ec x} dx$ .  |
| <b>Q.58</b> | Evaluate: $\int_0^1 \cot^{-1}(1 - x + x^2) dx$ .   |
| <b>Q.59</b> | Evaluate: $\int_0^\pi \frac{x \sin x}{1 + \sin x} dx$ .  |
| <b>Q.60</b> | Evaluate: $\int_0^\pi x \sin x \cos^4 x dx$ .  |
| <b>Q.61</b> | Evaluate: $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$ .                            |
| <b>Q.62</b> | Prove that $\int_0^{\pi/2} \log \sin x dx = \int_0^{\pi/2} \log \cos x dx = -\frac{\pi}{2} \log 2$ .   |
| <b>Q.63</b> | Evaluate: $\int_0^\pi \log(1 + \cos x) dx$ .   |

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| <b>Q.64</b> | Evaluate: $\int_0^\pi \frac{x \tan x}{\sec x + \tan x} dx$ .                                     |
| <b>Q.65</b> | Evaluate: $\int_0^{\pi/2} \frac{\sin x - \cos x}{1 + \sin x \cos x} dx$ .                        |
| <b>Q.66</b> | Evaluate: $\int_0^{\pi/2} (2 \log \sin x - \log \sin 2x) dx$ .                                   |
| <b>Q.67</b> | Evaluate: $\int_0^1 x(1-x)^n dx$ .   |
| <b>Q.68</b> | Evaluate: $\int_0^{\pi/2} \frac{\sin x \cos x}{1 + \sin^4 x} dx$ .                               |
| <b>Q.69</b> | Evaluate $\int_0^{\pi/2} \frac{\cos x}{\left(\cos \frac{x}{2} + \sin \frac{x}{2}\right)^3} dx$ . |
| <b>Q.70</b> | Evaluate: $\int_0^{\pi/4} \frac{\tan^3 x}{1 + \cos 2x} dx$ .                                     |
| <b>Q.71</b> | Evaluate $\int_0^1 \frac{1-x^2}{x^4+x^2+1} dx$ .   |
| <b>Q.72</b> | Evaluate: $\int_0^{\pi/2} \frac{\cos x}{1+\cos x+\sin x} dx$ .                                   |
| <b>Q.73</b> | Evaluate $\int_0^{\pi/2} \sqrt{\cos \theta} \sin^3 \theta d\theta$ .                             |
| <b>Q.74</b> | Evaluate $\int_0^{\pi/2} \frac{\cos \theta}{(1+\sin \theta)(2+\sin \theta)} d\theta$ .           |
| <b>Q.75</b> | Evaluate $\int_0^1 \frac{x \tan^{-1} x}{(1+x^2)^{3/2}} dx$ .                                     |
| <b>Q.76</b> | Evaluate $\int_0^{1/\sqrt{2}} \frac{\sin^{-1} x}{(1-x^2)^{3/2}} dx$ .                            |

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| <b>Q.77</b> | Evaluate $\int_0^{\pi/4} \frac{\sin x + \cos x}{9 + 16 \sin 2x} dx$ .   |
| <b>Q.78</b> | Evaluate: $\int_0^1 \frac{\log(1+x)}{(1+x^2)} dx$ .   |
| <b>Q.79</b> | Evaluate: $\int_0^{\pi/2} (\sqrt{\tan x} + \sqrt{\cot x}) dx$ .   |
| <b>Q.80</b> | Evaluate $\int_0^{\pi} \frac{1}{5+4\cos x} dx$ .  |
| <b>Q.81</b> | <b>Evaluate:</b> $\int_{-1}^1 f(x) dx$ , where $f(x) = \begin{cases} 1-2x, & \text{when } x \leq 0 \\ 1+2x, & \text{when } x \geq 0 \end{cases}$ .  |
| <b>Q.82</b> | <b>Evaluate:</b> $\int_1^3 f(x) dx$ , where $f(x) = \begin{cases} x-8, & \text{when } 1 \leq x \leq 2 \\ -2x, & \text{when } 2 \leq x \leq 3 \end{cases}$ .   |
| <b>Q.83</b> | <b>Evaluate:</b> $\int_0^9 f(x) dx$ , where $f(x) = \begin{cases} \sin x, & \text{when } 0 \leq x \leq \frac{\pi}{2} \\ 1, & \text{when } \frac{\pi}{2} \leq x \leq 5 \\ e^{x-5}, & \text{when } 5 \leq x \leq 9 \end{cases}$ . |
| <b>Q.84</b> | <b>Evaluate:</b> $\int_0^4  x^2 - 5x + 6  dx$   |
| <b>Q.85</b> | <b>Evaluate:</b> $\int_0^{\frac{\pi}{2}}  \sin x - \cos x  dx$ .  |
| <b>Q.86</b> | <b>Evaluate:</b> $\int_1^4 f(x) dx$ , where $f(x) =  x-1  +  x-2  +  x-3 $ .  |
| <b>Q.87</b> | <b>Evaluate:</b> $\int_{-1}^2 f(x) dx$ , where $f(x) =  x+1  +  x  +  x-1 $ .   |

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| <b>Q.88</b> | <b>Evaluate:</b> $\int_{-\pi}^{\frac{\pi}{2}} (\sin x  - \cos x ) dx$                                    |
| <b>Q.89</b> | <b>Evaluate:</b> $\int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} (2\sin x  + \cos x ) dx$ .                       |
| <b>Q.90</b> | <b>Evaluate:</b> If $\int_a^b x^3 dx = 0$ and $\int_a^b x^2 dx = \frac{2}{3}$ , find the value of a & b? |
| <b>Q.91</b> | <b>Evaluate:</b> $\int_0^{\frac{\pi}{2}} \frac{\cos x}{5+4\sin x} dx$ .                                  |
| <b>Q.92</b> | <b>Evaluate:</b> $\int_0^{\frac{\pi}{4}} \frac{\sin 2x}{\sin^4 x + \cos^4 x} dx$                         |
| <b>Q.93</b> | <b>Evaluate:</b> $\int_0^1 x \sqrt{\frac{1-x^2}{1+x^2}} dx$  |
| <b>Q.94</b> | <b>Evaluate:</b> $\int_0^{\frac{\pi}{4}} \frac{\sin x + \cos x}{9+16\sin 2x} dx$                         |
| <b>Q.95</b> | <b>Evaluate:</b> $\int_0^{\frac{\pi}{2}} \frac{\sin x \cos x}{\cos^2 x + 3\cos x + 2} dx$                |
| <b>Q.96</b> | <b>Evaluate:</b> $\int_0^1 x \tan^{-1} x dx$   |
| <b>Q.97</b> | <b>Evaluate:</b> $\int_0^{\frac{1}{2}} \frac{\sin^{-1} x}{(1-x^2)^{\frac{3}{2}}} dx$                     |
| <b>Q.98</b> | <b>Evaluate:</b> $\int_0^{\frac{\sqrt{2}}{2}} \frac{\sin^{-1} x}{(1-x^2)^{\frac{3}{2}}} dx$              |

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| <b>Q.99</b>  | <b>Evaluate:</b> $\int_0^1 \sin^{-1} \left( \frac{2x}{1+x^2} \right) dx$                    | <b>Q.112</b>  | <b>Evaluate:</b> $\int_0^\pi x \sin x \cos^4 x dx$  |
| <b>Q.100</b> | <b>Evaluate:</b> $\int_0^\infty \frac{x \tan^{-1} x}{(1+x^2)^2} dx$                         | <b>Q.113</b>  | <b>Evaluate:</b> $\int_0^\pi \frac{x \sin x}{1+\cos^2 x} dx$  |
| <b>Q.101</b> | <b>Evaluate:</b> $\int_0^{\pi/2} \frac{\sqrt{\sec x}}{\sqrt{\sec x} + \sqrt{\cos ec x}} dx$ | <b>Q.114</b>  | <b>Evaluate:</b> $\int_0^{\pi/2} \frac{x}{1+\sin x + \cos x} dx$                                    |
| <b>Q.102</b> | <b>Evaluate:</b> $\int_0^5 \frac{\sqrt[4]{x+4}}{\sqrt[4]{x+4} + \sqrt[4]{9-x}} dx$          | <b>Q.115</b>  | <b>Evaluate:</b> $\int_0^\pi \frac{x}{1+\cos^2 x} dx$   |
| <b>Q.103</b> | <b>Evaluate:</b> $\int_0^\pi \sin^{2m} x \cos^{2m+1} x dx$                                  | <b>Q.116</b>  | <b>Evaluate:</b> $\int_0^{\pi/2} \frac{x \sin 2x}{\cos x + \sin x} dx$                              |
| <b>Q.104</b> | <b>Evaluate:</b> $\int_0^{2\pi} \frac{\sin 2\theta}{a-b \cos \theta} d\theta$               | <b>Q.117</b>  | <b>Evaluate:</b> $\int_0^{\pi/2} \frac{\sin^2 x}{\cos x + \sin x} dx$                               |
| <b>Q.105</b> | <b>Evaluate:</b> $\int_0^{\pi/2} \sin 2x \log \tan x dx$                                    | <b>Q.118</b>  | <b>Evaluate:</b> $\int_0^{\pi/2} \frac{\cos x}{1+\cos x + \sin x} dx$                               |
| <b>Q.106</b> | <b>Evaluate:</b> $\int_0^1 \log \left( \frac{1}{x} - 1 \right) dx$                          | <b>Q.119</b>  | <b>Evaluate:</b> $\int_0^{\pi/2} (2 \log \sin x - \log \sin 2x) dx$                                 |
| <b>Q.107</b> | <b>Evaluate:</b> $\int_0^{\pi/2} \frac{x}{\sin x + \cos x} dx$                              | <b>Q.120</b>  | <b>Evaluate:</b> $\int_{-\frac{3}{2}}^3 \frac{\sqrt{5-x}}{\sqrt{x} + \sqrt{5-x}} dx$                |
| <b>Q.108</b> | <b>Evaluate:</b> $\int_0^\pi \frac{x \tan x}{\sec x + \tan x} dx$                           | <b>Q.121</b>  | <b>Evaluate:</b> $\int_{\frac{5}{2}}^5 \frac{\sqrt{x}}{\sqrt{x} + \sqrt{7-x}} dx$                   |
| <b>Q.109</b> | <b>Evaluate:</b> $\int_0^{2\pi} \frac{x \cos x}{1+\cos x} dx$                               | <b>Q.122</b>  | <b>Evaluate:</b> $\int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \frac{1}{1+\sqrt{\cot x}} dx$                |
| <b>Q.110</b> | <b>Evaluate:</b> $\int_0^\pi \frac{x \tan x}{\sec x \cos ec x} dx$                          | <b>Q.123</b>  | <b>Evaluate:</b> $\int_{-\frac{3\pi}{4}}^{\frac{3\pi}{4}} \frac{\sqrt{\tan x}}{1+\sqrt{\tan x}} dx$ |
| <b>Q.111</b> | <b>Evaluate:</b> $\int_0^{\pi/2} \frac{x \sin x \cos x}{\sin^4 x + \cos^4 x} dx$            | <b>Q.124</b> If $f(x)$ is a continuous function defined |   |

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|                                | on $\int_{-a}^a f(x)dx = \begin{cases} 2 \int_0^a f(x)dx, & \text{if } f(-x) = f(x) \\ 0, & \text{if } f(-x) = -f(x) \end{cases}$ . Prove it .                   |
| Q.125                          | <b>Evaluate:</b> $\int_{-\pi/4}^{\pi/4} x^4 \sin x dx$<br>*****  |
| <b>AREA BOUNDED BY A CURVE</b> |  |
| *****                          |  |
| Q.1                            | Make a rough sketch of the region, given below and find its area using integration. $\{(x, y) : 0 \leq y \leq x^2 + 1; 0 \leq y \leq x + 1; 0 \leq x \leq 2\}$ . |
| Q.2                            | Find the area of the region bounded by the two parabolas $x^2 = y$ & $y^2 = x$ .   |
| Q.3                            | Using integration, find the area of the triangle bounded by the lines $x + 2y = 2$ , $y - x = 1$ and $2x + y = 7$ .  |
| Q.4                            | Find the area of the region bounded by $y^2 = 4x$ , $x = 1$ , $x = 4$ and x-axis in the first quadrant.  |
| Q.5                            | Using integration, find the area of the triangle bounded by the lines $y = 2x + 1$ , $y = 3x + 1$ and $x = 4$ .  |
| Q.6                            | Find the area of the region bounded by the curve $y^2 = 4a^2(x - 1)$ and the lines $x = 1$ & $y = 4a$ .  |
| Q.7                            | Find the area of the region enclosed between the curves $y = \sin x$ & $y = \cos x$ for $0 \leq x \leq \frac{\pi}{2}$ .  |
| Q.8                            | Sketch the region common to the parabola $y = 2x - x^2$ and the line $y = -x$ . Also, find the area of the region using integration.                             |
| Q.9                            | Sketch the graph $y = 1 +  x + 1 $ . Evaluate $\int_{-3}^3 [1 +  x + 1 ] dx$ . What does this value represent on the graph?                                      |
| Q.10                           |  |
| Q.11                           | Find the area of the smaller region bounded by the ellipse $9x^2 + 25y^2 = 225$  |

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|      | and the line $3x + 5y = 15$ .  |
| Q.12 | Find the area of the region $\{(x, y) : x^2 + y^2 \leq 2ax, y^2 \geq ax, x \geq 0, y \geq 0\}$ .   |
| Q.13 | Draw a rough sketch of $y^2 = x + 1$ and $y^2 = -x + 1$ and determine the area enclosed by the two curves.   |
| Q.14 | Prove that the curves $y^2 = 4x$ and $x^2 = 4y$ divide the area of the square bounded by $x = 0$ , $x = 4$ , $y = 4$ , $y = 0$ into three equal parts. |
| Q.15 | Using integration, find the area of the triangle whose vertices are A (2, 0), B (4, 5) and C (3, -2).  |
| Q.16 | Find the area bounded by the curves $y = 6x - x^2$ & $y = x^2 - 2x$ .  |
| Q.17 | Using integration, find the area bounded by the curve $x^2 = 4y$ and the straight line $x = 4y - 2$ .  |
| Q.18 | Sketch the region common to the circle $x^2 + y^2 = 16$ and the parabola $x^2 = 6y$ . Also, find the area of the region using integration.             |
| Q.19 | Using integration, find the area of the region curve $y = x^2 + 2$ , $y = x$ , $x = 0$ and $x = 3$ .   |
| Q.20 | Find the area of the region $\{(x, y) : x^2 + y^2 \leq 1 \leq x + y\}$ .   |
| Q.21 | Find the area of the region $\{(x, y) : x^2 \leq y \leq  x \}$ .   |
| Q.22 | Sketch the region bounded by $y = 2x - x^2$ and the x-axis and find its area using integration.  |
| Q.23 | Find the area of the region included between the parabolas $y^2 = 4ax$ & $x^2 = 4ay$ where $a > 0$ .   |
| Q.24 | Using integration, find the area of the two parabolas $4y^2 = 9x$ & $3x^2 = 16y$ . Also find the angle between two curves.                             |
| Q.25 | Using integration, find the area of the triangle whose vertices are A (3, 0), B (4, 6) and C (6, 2).   |
| Q.26 | Using integration, find the area of the region curve $y^2 = 4a^2(x - 3)$ and the lines $x = 3$ and $y = 4a$ .  |
| Q.27 | Find the area bounded by the curve $4x = y^2$ and the straight line  |

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|             | $2x = y + 4$ .  |   |
| <b>Q.28</b> | Make a rough sketch of the region given below and find its area using integration. $\{(x, y) : 0 \leq y \leq x^2 + 3; 0 \leq y \leq 2x + 3; 0 \leq x \leq 3\}$ .          | parabola $x^2 = 6y$ . Also, find the area of the region using integration.  |
| <b>Q.29</b> | Find the area of the region bounded by the curve $y^2 = 2y - x$ and the y-axis.   | <b>Q.39</b> Find the area of the smaller region bounded by the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ and the straight line $\frac{x}{a} + \frac{y}{b} = 1$ .            |
| <b>Q.30</b> | Find the area of the region $\{(x, y) : y^2 \leq 4x, 4x^2 + 4y^2 \leq 9\}$ .  | <b>Q.40</b> Sketch the region common to the circle $x^2 + y^2 = 25$ and the parabola $y^2 = 8x$ . Also, find the area of the region using integration.                            |
| <b>Q.31</b> | Find the area of the origin : $\{(x, y) : 0 \leq y \leq x^2, 0 \leq y \leq x+2; 0 \leq x \leq 3\}$ .  | <b>Q.41</b> Using integration find the area between curve $y^2 = x$ and the line $x + y = 2$ .  |
| <b>Q.32</b> | Find the area cut off the parabola $4y = 3x^2$ by the straight line $2y = 3x + 12$ .  | <b>Q.42</b> Using integration find the area between curve $y^2 = x$ and the line $x + y = 2$ and x axis .   |
| <b>Q.33</b> | Sketch the graph $f(x) = \begin{cases}  x - 2  + 2 & x \leq 2 \\ x^2 - 2 & x > 2 \end{cases}$ . Evaluate $\int_0^4 f(x)dx$ . What does this value represent on the graph? | <b>Q.43</b> Draw the rough sketch of the region enclosed between the circles $x^2 + y^2 = 9$ and $(x - 3)^2 + y^2 = 9$ . Using integration, find the area of the enclosed region. |
| <b>Q.34</b> | Find the area lying above x-axis and included between the circle $x^2 + y^2 = 2ax$ and the parabola $y^2 = ax$ .  | <b>Q.44</b> Find the area of the smaller region bounded by the ellipse $9X^2 + 16Y^2 = 114$ and the line $3x + 4y = 12$ .   |
| <b>Q.35</b> | Draw the rough sketch of the region enclosed between the circles $x^2 + y^2 = 4$ and $(x - 2)^2 + y^2 = 1$ . Using integration, find the area of the enclosed region .    | <b>Q.45</b> Using integration, find the area of the triangle whose vertices are A (2, 1), B (3,4) and C(5 , 2).   |
| <b>Q.36</b> | Using integration, find the area of the region $\{(x, y) :  x-1  \leq y \leq \sqrt{5-x^2}\}$ .<br>$= \frac{5\pi}{4} - \frac{1}{2}$  | <b>Q.46</b> Draw a rough sketch of the curves $y = \sin x$ & $y = \cos x$ as $x$ varies from 0 to $\frac{\pi}{2}$ and find the area of the region enclosed by them and Y- axis.   |
| <b>Q.37</b> | Using integration, find the area of the region enclosed between two circles $x^2 + y^2 = 1$ and $(x - 1)^2 + y^2 = 1$ .   | <b>Q.47</b> Using integration find the area of the region bounded by the parabola $y - 1 = x$ , x axis and the line $x = -2$ and $x = 3$ .  |
| <b>Q.38</b> | Sketch the region common to the circle $x^2 + y^2 = 16$ and the   | <b>Q.48</b> Show that the area enclosed by the circle $x^2 + y^2 = 64a^2$ and the parabola $y^2 = 12ax$ is $a^2 \left( \frac{16}{\sqrt{3}} + \frac{64\pi}{3} \right)$             |
|             |   | <b>Q.49</b> Using integration, find the area of the triangle bounded by the lines $4 = 2x + y$ , $2y = 3x - 6$ and $x - 3 y + 5 = 0$ .  |
|             |   | <b>Q.50</b> Using integration find the area bounded by the curve $ x  +  y  = 1$ .  |
|             |   | <b>Q.51</b> Draw a rough sketch of the curve $y = \sqrt{3x + 4}$ between $x = 0$ and $x = 4$ and find the area under the curve and above the x-axis.                              |
|             |   | <b>Q.52</b> Draw a rough sketch of the curves $y = \sin x$ & $y = \cos x$ as $x$ varies from 0 to   |

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|             | $\frac{\pi}{2}$ and find the area of the region enclosed by them and (i) x – axis (ii) y axis (iii) $x = 0$ & $x = \frac{\pi}{2}$ .                           |
| <b>Q.53</b> | Using integration, find the area lying above x-axis and included between the circle $x^2 + y^2 = 8x$ and interior of the parabola $y^2 = 4x$ .                |
| <b>Q.54</b> | Using integration, find the area lying above x-axis and included between the circle $x^2 + y^2 = 8x$ and the parabola $y^2 = 4x$ .                            |
| <b>Q.55</b> | Sketch the region lying in the first quadrant and bounded by $y = 4x^2$ , $x = 0$ , $y = 1$ and $y = 4$ . Find the area of the region using integration . ans |
| <b>Q.56</b> | In fig. AOBA is a part of the ellipse $9x^2 + y^2 = 36$ in the first quadrant such that OA=2 and OB=6. Find the area between the arc AB and the chord AB.     |
|             |   |
| <b>Q.57</b> | Evaluate the area of the region bounded by the curve $y = 2\sqrt{1-x^2}$ and the x-axis , after drawing a rough sketch of the same .                          |
| <b>Q.58</b> | Find the area lying above x-axis and included between the circle $x^2 + y^2 = 2ax$ and the parabola $y^2 = ax$ .  |
| <b>Q.59</b> | Find the ratio of the areas into which curve $y^2 = 6x$ divides the region bounded by $x^2 + y^2 = 16$ .  |
| <b>Q.60</b> | Using integration find the area of the region bounded by the parabola $x^2 + y^2 = 4$ , x axis and the line $x = \sqrt{3}y$ in the first quadrant .           |
| <b>Q.61</b> | Find the area of the region bounded by the line $2y=-x+8$ , the x-axis and the lines $x=2$ and $x=4$ .  |
| <b>Q.62</b> | Find the area of the region bounded by the curve $y=x$ , the x-axis and the ordinates   |

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|             | $x=-1$ and $x=2$ .  |
| <b>Q.63</b> | Find the area of the region bounded by the parabola $y^2 = 4x$ and its latus rectum.  |
| <b>Q.64</b> | Calculate the area of the region bounded by the curve $y = 2\sqrt{1-x^2}$ and the x-axis from $x=0$ to $x=1$ .                |
| <b>Q.65</b> | Find the area of the region bounded by the curve $y = \sqrt{3x+4}$ , above the x-axis and between the lines $x=0$ and $x=4$ . |
| <b>Q.66</b> | Find the area of the region bounded by the curve $y^2 = 4x$ and the straight line $y=2x-4$ .                                  |
|             | *****// *****   |