

Sample Paper – 2013
Class – X
Subject – Mathematics

Time: 3 hours

Maximum marks: 90

Section - A

1. Which of the following will have a terminating decimal expansion?

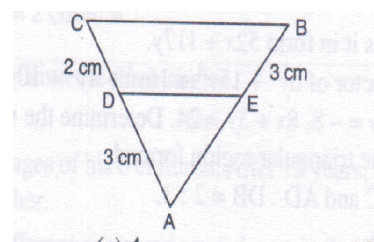
- (a) $77 / 210$
- (b) $23 / 330$
- (c) $125 / 441$
- (d) $57 / 8$

2. If $(x + 1)$ is a factor of $x^2 - 3ax + 3a - 7$, then the value of a is

- (a) 1
- (b) -1
- (c) 0
- (d) -2

3. In the adjoining figure, $DE \parallel CB$. What is the length of AE ?

- (a) 5
- (b) 4.5
- (c) 4
- (d) 3



4. If θ is an acute angle and $\cos \theta = 9 / 41$, then the value of $\tan \theta$ is

- (a) $40 / 41$
- (b) $9 / 40$
- (c) $40 / 9$
- (d) $9 / 41$

5. $9 \sec^2 A - 9 \tan^2 A$ is equal to

- (a) 0
- (b) 1
- (c) 9
- (d) -9

6. The class mark of a class interval is equal to

- (a) lower limit + upper limit
- (b) upper limit - lower limit
- (c) 2 (upper limit - lower limit)
- (d) 2 (upper limit + lower limit)

7. The value of $\sin^2 5^\circ + \sin^2 10^\circ + \sin^2 15^\circ + \dots + \sin^2 90^\circ$ is equal to
- 8
 - 8.5
 - 9
 - 9.5
8. If $0 < \theta < 90^\circ$, then $\sec \theta$ is
- >1
 - <1
 - $=1$
 - 0

SECTION-B

Question number 9 to 14 carry 2 marks each.

9. If $\sec 4A = \operatorname{cosec} (A - 20^\circ)$ where $4A$ is an acute angle, find the value of A .
10. Write the following distribution as more than type cumulative frequency distribution:

Class interval	50-55	55-60	60-65	65-70	70-75	75-80
Frequency	2	6	8	14	15	5

11. Two poles of height 10 m and 15 m stand vertically on a plane ground. If the distance between their feet is $5\sqrt{3}$ m, find the distance between their tops.
12. Use Euclid's division algorithm to find H.C.F. of 870 and 225.
13. α, β are the roots of the quadratic polynomial $P(x) = x^2 - (k + 6)x + 2(2k - 1)$. Find the value of k , if $\alpha + \beta = \frac{1}{2} \alpha\beta$
14. Solve: $37x + 43y = 123, 43x + 37y = 117$.

OR

Solve: $x + \frac{6}{y} = 6$ and $3x - \frac{8}{y} = 5$ SECTION-C

Question number 15 to 24 carry 3 marks each.

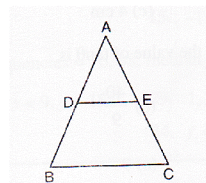
15. Find the LCM and HCF of 510 and 92 and verify that $\text{LCM} \times \text{HCF} = \text{product of the two numbers}$.

Or

Find the HCF of 52 and 117 and express it in form $52x + 117y$.

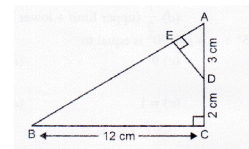
16. Using division show that $3y^2 + 5$ is a factor of $6y^5 + 15y^4 + 16y^3 + 4y^2 + 10y - 35$.
17. Draw the graphs of the equations $2x - y = -8$, $8x + 3y = 24$. Determine the vertices of the triangle by the lines representing these equations and the x-axis. Shade the triangular region formed.

18. In the given figure, DE is parallel to BC and AD: DB = 2: 3.
Determine area ($\triangle ADE$) : area ($\triangle ABC$).



Or

- In the given figure, ABC is a right-angled triangle at C. Prove that $\triangle ABC \sim \triangle ADE$ and find the lengths of AE and DE.



19. If $\cos A = .12 / 13$, then verify that $\sin A(1 - \tan A) = 35 / 156$
20. ABC is a triangle and PQ is a straight line meeting AB in P and AC in Q. If AP = 1 cm, PB = 3 cm, AQ = 1.5 cm, QC = 4.5 cm. Prove that area of MPQ is one-sixteenth of the area of $\triangle ABC$.
21. Evaluate: $\cot \theta \cdot \tan (90^\circ - \theta) - \sec (90^\circ - \theta) \operatorname{cosec} \theta + \sin^2 25^\circ + \sin^2 65^\circ + \sqrt{3} \tan 6^\circ \tan 16^\circ \tan 74^\circ \tan 84^\circ$.

Or Show that: $(\tan A + \operatorname{cosec} B)^2 - (\cot B - \sec A)^2 = 2 \tan A \cot B (\operatorname{cosec} A + \sec B)$.

22. Calculate the median for the following data:

Class	20-40	40-60	60-80	80-100	100-120	120-140	140-160
Frequency	12	15	23	18	12	12	8

23. The ages of employees in two factories A and B are given below:

Age of Employees (in Years)		20-30	30-40	40-50	50-60	60-70
Number of Employees in Factories	A	5	26	78	104	98
	B	8	40	58	90	83

Find the modal age of employees in factory A and factory B.

24. Prove that $5 + \sqrt{2}$ is an irrational number.

SECTION-D

Question number 25 to 34 carry 4 marks each.

25. Prove that :
$$\frac{\cot \theta - 1 + \operatorname{cosec} \theta}{\cot \theta + 1 - \operatorname{cosec} \theta} = \frac{1}{\operatorname{cosec} \theta - \cot \theta}$$

OR

Prove that:
$$\sqrt{\frac{1 + \sin A}{1 - \sin A}} = \sec A + \tan A$$

26. If $\tan \theta + \sin \theta = m$ and $\tan \theta - \sin \theta = n$, show that $(m^2 - n^2)^2 = 16mn$

27. Find the mean of following distribution by step deviation method.

Daily Expenditure	100-150	150-200	200-250	250-300	300-350
No. of householders	4	5	12	2	2

28. Draw 'less than Ogive' for the following frequency distribution and hence obtain the median.

Marks obtained	10-20	20-30	30-40	40-50	50-60	60-70	70-80
No. of students	3	4	3	3	4	7	9

29. Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.

OR

Prove that in a triangle, if square of one side is equal to the sum of the squares of the other two sides, then the angle opposite the first side is a right angle.

30. Nine times a two-digit number is the same as twice the number obtained by interchanging the digits of the number. If one digit of the number exceeds the other number by 7, find the number.

31. Solve the following system of equations graphically and find the vertices of the triangle formed by these lines and the x-axis.

$$4x - 3y + 4 = 0, 4x + 3y - 20 = 0$$

32. Find all the zeroes of the polynomial $x^4 - 5x^3 + 2x^2 + 10x - 8$, if two of its zeroes are $\sqrt{2}, -\sqrt{2}$.

33. Use Euclid's division lemma to show that the square of any positive integer is either of the form $3m$ or $3m + 1$ for some integer m .

34. In a $\triangle ABC$, the angles at B and C are acute. If BE and CF are drawn perpendicular on AC and AB respectively, prove that: $BC^2 = AB \times BF + AC \times CE$

