

Sample Paper – 2011
Class – XI
Subject – Mathematics

Time: 3Hrs.

Max. Marks: 100

General Instructions: (The question paper has two printed pages divided in 29 questions as under)

- ❖ All the questions are compulsory.
- ❖ The question paper has been divided in 3 sections A, B and C.
- ❖ Section A contains 10 questions of 1 mark each.
- ❖ Section B contains 12 questions of 4 marks each.
- ❖ Section C contains 7 questions of 6 marks each.
- ❖ There is no overall choice however internal choice has been provided in section B & C.
- ❖ Use of calculators is not permitted.

Section – A

1. Write the set $A = \{1, 4, 9, 16, \dots\}$ in set builder form.
2. If $(x+1, y-2) = (3, 1)$ find the value of x and y .
3. Find the value of $\tan\left(\tan^{-1}\frac{19\pi}{3}\right)$.
4. Convert the complex number $(1+i)$ in polar form.
5. Find the value of n if ${}^{n-1}P : {}^n P = 1 : 9$.
6. Find the sum of 'n' terms of the series: $\frac{1}{1 \times 2} + \frac{1}{2 \times 3} + \frac{1}{3 \times 4} + \dots$.
7. Find the equation of the line through $(-2, 3)$ with slope -4 .
8. Write the converse of the following statement, "If a number n is even, then n^2 is even".
9. Write the contra positive of the statement "If a triangle is equilateral, it is isosceles".
10. Evaluate $\lim_{x \rightarrow 0} \frac{\sin ax}{\sin bx}$.

Section – B

11. For $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ $A = \{2, 4, 6, 8\}$ $B = \{2, 3, 5, 7, 8\}$ verify DeMorgan's Law

i.e. $(A \cup B)' = A' \cap B'$ and $(A \cap B)' = A' \cup B'$

12. Let $f(x) = x^2$ and $g(x) = 2x + 1$ be two real functions, find $(f+g)(x)$, $(f-g)(x)$, $(f \cdot g)(x)$ and $\frac{f}{g}(x)$.

13. Prove that $\cot x \cot 2x - \cot 2x \cot 3x - \cot 3x \cot x = 1$

Or

If $\tan x = \frac{3}{4}$, $\pi < x < \frac{3\pi}{2}$, find the value of $\sin \frac{x}{2}$, $\cos \frac{x}{2}$ and $\tan \frac{x}{2}$.

14. If $(x + iy)^3 = u + iv$ prove that $\frac{u}{x} + \frac{v}{y} = 4(x^2 - y^2)$.

15. In how many of the distinct permutations of the letter **MISSISSIPPI** do the for 'I's not come together?

Or

P.T.O.

A committee of 7 members has to be formed from 9 boys and 4 girls. In how many ways can this be done, when the committee consists of (i) exactly 3 girls (ii) at least 3 girls (iii) at most 3 girls?

16. Find the term independent of 'x' in the expansion of $\left(\frac{3x^2}{2} - \frac{1}{3x}\right)^6$.

17. The sum of the first three terms of a G.P. is $\frac{13}{12}$ and their product is -1 . Find the common ratio and the terms.

18. The lines through the points (4, 3) and (h, 1) intersect the line $7x - 9y - 19 = 0$ at right angle. Find the value of 'h'.

Or

Find the coordinates of the foot of the perpendicular from the point (-1, 3) to the line $3x - 4y = 16$.

19. Find the equation of the circle passing through the points (4, 1) and (6, 5) whose centre lies on the line $4x + y = 16$.

20. Using section formula, prove that the three points (4, 6, 10), (2, 4, 6) and (14, 0, -2) are collinear.

21. Compute the derivative of $\tan x$ using first principle.

22. A box contains 10 red, 20 blue and 30 green marbles. 5 marbles are drawn from the box. What is the probability that (i) all will be blue (ii) at least one will be green.

Section – C

23. A college awarded 38 medals on foot-ball, 15 in basket-ball and 20 in cricket. If these medals went to a total of 58 men and only 3 men received medal in all three sports, how many received medals is there in exactly two of the three sports.

24. Use mathematical induction for the series to prove that

$$1.3 + 3.5 + 5.7 + \dots + (2n - 1)(2n + 1) = n \left(\frac{4n^2 + 6n - 1}{3} \right).$$

Or

$$1^2 + 3^2 + 5^2 + \dots + (2n - 1)^2 = \frac{n(2n - 1)(2n + 1)}{3}.$$

25. Solve the following system of inequalities graphically: $x + 2y \leq 10$, $x + y \geq 1$, $x - y \leq 0$, $x \geq 0$, $y \geq 0$.
26. The coefficient of the $(r - 1)^{\text{th}}$, r^{th} and $(r + 1)^{\text{th}}$ terms in the expansion of $(x + 1)^n$ are in the ratio 1:3:5. Find 'n' and 'r'.
27. Find the coordinates of the foci, the vertices, the length of major, minor axis, the eccentricity and the length of latus rectum for the ellipse $36x^2 + 4y^2 = 144$. **Or**
Find the equation of the hyperbola whose foci is $(0, \pm\sqrt{10})$, passing through the point (2,3).
28. The ratio of the sums of m and n terms of an AP is $m^2 : n^2$. Show that the ratio of m^{th} and n^{th} term is $(2m - 1) : (2n - 1)$
29. Find the mean and the standard deviation using the short cut method.

X	60	61	62	63	64	65	66	67	68
frequency	2	1	12	29	25	12	10	4	5

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