

PROBLEMS on MATRIX

1. If $A = \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix}$, and $A^2 = mA$, then write the value of m . [1]
 2. If a matrix has 15 elements, then write all possible order it can have. [1]
 3. If C_{ij} is the cofactor of the element a_{ij} of the determinant $\begin{vmatrix} 2 & -3 & 5 \\ 6 & 0 & 4 \\ 1 & 5 & -7 \end{vmatrix}$ then write the value of $a_{32}C_{32}$. [1]
 4. A is a square matrix of order 3 and $|A| = 7$. Write the value of $|\text{Adj } A|$. [1]
 5. Write the adjoint of the following matrix: $\begin{bmatrix} 2 & -1 \\ 4 & 3 \end{bmatrix}$. [1]
 6. For what value of x , is the matrix $A = \begin{pmatrix} 0 & 1 & -2 \\ -1 & 0 & 3 \\ x & -3 & 0 \end{pmatrix}$ a skew-symmetric matrix? [1]
 7. If $A = \begin{bmatrix} 2 & -3 \\ 3 & 4 \end{bmatrix}$, show that $A^2 - 6A + 17I = O$. Hence find A^{-1} . [4]
 8. If $A = \begin{pmatrix} 2 & 0 & 1 \\ 2 & 1 & 3 \\ 1 & -1 & 0 \end{pmatrix}$, then find the value of $A^2 - 3A + 2I$. [4]
 9. Express the following matrix as the sum of a symmetric and a skew symmetric matrix. $\begin{bmatrix} 1 & 3 & 5 \\ -6 & 8 & 3 \\ -4 & 6 & 5 \end{bmatrix}$ [4]
 10. Using matrices solve the following system of equations : $\begin{matrix} 4x + 3y + 2z = 60 \\ x + 2y + 3z = 45 \\ 6x + 2y + 3z = 70 \\ 2x - 3y + 5z = 11 \end{matrix}$ [6]
- OR,
- Using matrices solve the following system of equations : $\begin{matrix} 3x + 2y - 4z = -5 \\ x + y - 2z = -3 \end{matrix}$
11. Find the inverse of the following matrix using elementary operations $A = \begin{pmatrix} 1 & 2 & -2 \\ -1 & 3 & 0 \\ 0 & -2 & 1 \end{pmatrix}$ [6]

“The essence of Mathematics, lies in its freedom” – CANTOR

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