Series : PTS/2  
Roll No. 2 1 4 1 2  
Candidates must write the Code on the title page of the answer-book.  
**PLEASURE TEST SERIES XII - 02**  
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For more stuffs on Maths, please visit : www.theOPGupta.com  
Time Allowed : 180 Minutes  
**SECTION A**  
Q01. Let A = (d<sub>1</sub> d<sub>2</sub> d<sub>3</sub> ... d<sub>n</sub>) be a diagonal matrix. What is the value of det (A)?  
Q02. If A = 
$$\begin{bmatrix} 2 & 3 \\ k & 2 \end{bmatrix}$$
 and A. adjA = 13 1 then, find the value of k.  
Q03. Under what condition (A = B) (A + B) is equal to A<sup>2</sup> = B<sup>2</sup> such that orders of A and B are same?  
Q04. Let f : R → R be defined by f(x) = (3 - x<sup>3</sup>)<sup>13</sup>. Determine for (x).  
Q05. If the plane 4x + 4y -  $\lambda z = 0$  contains the line  $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z}{4}$ , find the value of  $\lambda$ .  
Q06. Evaluate the integral of  $\int \frac{\sqrt{5+x^{30}}}{x^{4/5}} dx$ .  
**SECTION B**  
Q07. If a and b are two vectors such that 1a + b1= 1a1, then prove that vector 2a + b is perpendicular to vector  $\overline{b}$ .  
Q08. If  $xy\log(x+y) = 1$  then, prove that  $\frac{dy}{dx} = -\frac{y}{x}(\frac{x^2y + x + y}{x^{2y} + x + y})$ .  
**OR** If  $y = \sqrt{x^2 + 1} - \log(\frac{1}{x} + \sqrt{1 + \frac{1}{x}})$  then, prove that  $\frac{dy}{dx} = \frac{\sqrt{x^2 + 1}}{x}$ .  
Q09. (i) Fvaluate : sin cos<sup>-1</sup>(1) + cos sin<sup>-1</sup>(1).  
(ii) Find the value of m if the lines  $\frac{x+3}{3} = \frac{y-1}{5m} = \frac{z+4}{4}$  and  $\frac{x+1}{1} = \frac{y-4}{1} = \frac{z-4}{2}$  are perpendicular to each other.  
(iii) Find the integrating factor for the linear differential equation :  $(y^2 - 1) + 2xy\frac{dy}{dx} = (\frac{2}{y^2 - 1})\frac{dy}{dx}$ .  
Q10. A chairman is biased so that ha selects his relatives for a job 3 times as likely as others. If there are 3 posts for a job, find the probability distribution for selection of persons there than his relatives. If the chairman is biased then which value of if w will be demolished?  
Q11. Let  $f(x) = \begin{cases} x + \sqrt{2a}, 0 \le x = \pi/4 \\ 2x < ox x + 5 = \pi/4 < x \le \pi/2$  is a continuous function on  $0 \le x \le \pi$ . Then, determine the values of w with by.  
What are your views about "learning"? Is "learning" a continuous process?  
Q12. Solve : sin<sup>-5</sup>/{

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Let \* be a binary operation on N defined by a\*b = HCF of a and b. Is \* commutative? Is \* 014. associative? Does there exist identity for this binary operation on N? Let  $f: R \to R$  be defined as f(x) = 10x + 7. Find a function  $g: R \to R$  such that we OR have  $gof = fog = I_{R}$ .

- Express  $2\hat{i} \hat{j} + 3\hat{k}$  as the sum of a vector parallel and perpendicular to  $2\hat{i} + 4\hat{j} 2\hat{k}$ . Q15.
- Evaluate :  $\int \frac{x^4}{(x-1)(x^2-1)} dx$ . OR Evaluate :  $\int \frac{x^2 + \sin^2 x}{1+x^2} \sec^2 x dx$ . Q16. х  $\sin\theta$   $\cos\theta$
- With or without using the properties of determinants, evaluate :  $-\sin\theta -x = 1$  $\cos\theta = 1 = x$ Q17. Form the differential equation of the family of circles in  $2^{nd}$  quadrant and touching coordinate axes. Q18.
- Form the differential equation of the family of curves given by  $(a + bx) e^{y/x} = x$ . OR
- Find the equation of the plane parallel to x-axis and which contains the line of intersection of Q19. the palnes  $\vec{r}.(\hat{i} + \hat{j} + \hat{k}) = 1$  and  $\vec{r}.(2\hat{i} + 3\hat{j} - \hat{k}) + 4 = 0$ .

## **SECTION C**

- Two trainee carpenters A and B earn ₹150 and ₹200 per day respectively. A can make 6 frames and 4 Q20. stools per day while B can make 10 frames and 4 stools per day. How many days shall each work if it is desired to produce at least 60 frames and 32 stools at a minimum labour cost? Solve graphically.
- Triangle AOB is made in first quadrant of  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  where OA = a and OB = b. Find the area Q21. enclosed between the chord AB ad arc AB of ellipse. Being a student, comment on the following:

"Differentiate the wastage of seconds; integrate the number of hours in a day."

Q22. Find the distance of the point (2, 3, 4) from the plane 3x + 2y + 2z + 5 = 0 measured parallel to the

line 
$$\frac{x+3}{3} = \frac{y-2}{6} = \frac{z}{2}$$
.

Evaluate :  $\int \frac{\sqrt{1+x^2}}{1-x^2} dx$ . Q23.

Q24. A farmer wants to construct a circular well and a square garden in his field. He wants to keep sum of their perimeters fixed. Then prove that the sum of their areas is least when the side of square garden is double the radius of circular well. Do you think good planning can save energy, time and money?

**OR** Find the condition for the curves 
$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$
 and  $xy = c^2$  to intersect orthogonally.

Q25. Let X denote the number of colleges where you will apply after your results and P(X = x) denotes your probability of getting admission in x number of colleges. It is given that

$$P(X = x) = \begin{cases} kx, \text{ if } x = 0, \text{ or } 1\\ 2kx, \text{ if } x = 2\\ k(5-x), \text{ if } x = 3 \text{ or } 4 \end{cases}$$
, k is a positive constant.

Find the mean and variance of the probability distribution. 'College is actually life exposure.' How? Q26. For keeping fit, X people believe in morning walk, Y people believe in yoga and Z people join gym. Total no. of people are 70. Further 20%, 30% and 40% people are suffering from any diseases who believe in morning walk, yoga and gym respectively. Total number of such people is 21. If morning walk costs ₹0, yoga costs ₹500/month and gym costs ₹400/month and total expenditure is ₹23000. (i) Formulate a matrix problem. (ii) Calculate the number of each type of people.

**OR** Find the inverse of 
$$\begin{bmatrix} 1 & 2 & -2 \\ -1 & 3 & 0 \\ 0 & -2 & 1 \end{bmatrix}$$
 using elementary transformations.

## HINTS & ANSWERS for PTS XII - 02 [2014 - 2015]

the body of a person fit and healthy. **OR** 

 $\begin{bmatrix} 1 & 1 & 2 \\ 2 & 2 & 5 \end{bmatrix}$ 

Good Luck & God Bless You!