

# CLASS XII GUESS PAPER MATHEMATICS

**Total Marks -100.**

**Time- 3h**

Section – A, One marks each, Section – B, four marks Each, Section – C, Six marks each

### SECTION-A

1. Find the possible orders of the matrices having 12 elements?
2. Show that the function  $f(x) = x^3 + 3x^2 + 3x - 7$  is always increasing on  $\mathbb{R}$ .
3. Evaluate  $\int_1^{1.9} [x] dx$
4. Probability of a success in an experiment of four trials is  $\frac{1}{3}$ . Find the probability of no success?
5. Find the projection of a vector  $2\hat{i} - \hat{j} + \hat{k}$  on the vector  $\hat{i} - 2\hat{j} + \hat{k}$ ?
6. differentiate  $\log_7 x$  with respect to  $x$ .

### SECTION-B

7. Prove that  $\tan^{-1}\left(\frac{2x}{1-x^2}\right) + \tan^{-1}x = \tan^{-1}\left(\frac{3x-x^3}{1-3x^2}\right)$
8. If the function  $f: \mathbb{R} \rightarrow \mathbb{R}$  given by  $f(x) = x^2 + 3x + 1$  and  $g: \mathbb{R} \rightarrow \mathbb{R}$  given by  $g(x) = 2x - 1$ , then find  $g \circ f$  and  $f \circ g$ ? **OR**

Let  $A = \{x \in \mathbb{R} : -1 \leq x \leq 1\} = B$  show that  $f: A \rightarrow B$ , given by  $f(x) = x|x|$  is bijective.

9. Using the properties of determinant show that 
$$\begin{vmatrix} (b+c)^2 & a^2 & a^2 \\ b^2 & (c+a)^2 & b^2 \\ c^2 & c^2 & (a+b)^2 \end{vmatrix} = 2abc(a+b+c)^3$$
10. Find the value of  $k$  for which the function  $f(x) = \begin{cases} 2x-1, & x < 2 \\ k, & x = 2 \\ 3x-1, & x > 2 \end{cases}$  is continuous at  $x=2$
11. Differentiate w.r.t  $x$ ,  $y = \tan^{-1}\left(\frac{\sqrt{1+x}-\sqrt{1-x}}{\sqrt{1+x}+\sqrt{1-x}}\right)$

**OR**

Find the interval for which the function  $f(x) = x^3 - 12x^2 + 36x + 17$  is increasing or decreasing

12. Find the equation of the tangent to the curve  $y = \sqrt{3x - 2}$ , which is parallel to the line  $4x - 2y + 5 = 0$

13. Evaluate  $\int \frac{dx}{(x^2+1)(x^2+2)}$

14. Evaluate  $\int \frac{\cos 2x - \cos 2\alpha}{\cos x - \cos \alpha} dx$       **OR**      Evaluate  $\int_0^{\frac{\pi}{2}} \frac{\sin^{\frac{3}{7}} x}{\sin^{\frac{3}{7}} x + \cos^{\frac{3}{7}} x} dx$

15. Find the unit vector perpendicular to the vectors  $(3\vec{a} + \vec{b})$  &  $(\vec{a} - 2\vec{b})$  where  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$ , and  $\vec{b} = 4\hat{i} - 2\hat{j} + 3\hat{k}$

16. Find the coordinate of point, where the line  $\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{2}$  intersect the plane  $x - y + z - 5 = 0$ , also find the angle between them. **OR**

Find the equation of the plane passing through the points  $(1,1,2)$ ;  $(3,2,1)$  &  $(-3,-4,-5)$ .

17. Solve the differential equation  $x \frac{dy}{dx} \sin\left(\frac{y}{x}\right) + x - y \sin\left(\frac{y}{x}\right) = 0$

18. The probabilities of A,B,C can solve a given problem are  $\frac{1}{3}, \frac{3}{5}, \frac{3}{8}$  respectively. If all the three try to solve the problem simultaneously, find the probability that at least one of them can solve the problem?

19. Evaluate  $\int \sqrt{\frac{1+\cos 2x}{1-\cos 2x}} dx$

**SECTION-B**

20. Solve the Equations  $2x + y + z = 7$ ;  $x - y - z = -4$ ;  $3x + 2y + z = 10$

**OR** Find the Inverse of the matrix by using elementary operation  $\begin{bmatrix} -1 & 3 & 3 \\ 5 & 2 & 1 \\ 1 & -2 & 4 \end{bmatrix}$

21. Show that the right circular cone of least curve surface area and given volume has an altitude equal to  $\sqrt{2}$  times the radius of the base.

22. Evaluate  $\int_0^{\frac{\pi}{2}} \log \sin x dx$

23. Draw a rough sketch of  $(x, y \geq 0)$ ,  $y^2 \geq 4x$  and  $x^2 \geq 4y$ , and find the area of the bounded region by using integration **OR**, Evaluate by using limit as sum  $\int_1^3 (x^2 - x + 1) dx$

24. Find the equation of the plane through the line of intersection of the planes  $x + y + z = 1$  and  $2x + 3y + 4z = 5$  which is perpendicular to the plane  $3x - 2y + 5z = 7$ , also find the distance of the plane from the origin?
25. A manufacture company makes two types of teaching aids A and B of Mathematics for class XII. Each type of A requires 9 labour hours of fabricating and 1 labour hour for finishing . Each type of B requires 12 labour hours of fabricating and 3 labour hour for finishing, fabricating and finishing the maximum labour available per week are 180 and 30 respectively. The company makes a profit of Rs 80 and Rs.120 on each pieces of A and B. how many pieces of A and B should be manufacture to get a maximum profit. Solve the problem by graphically. What is the maximum profit?
26. In a bulb factory machines A, B, C manufacture 60%, 30%, and 105 bulbs, respectively. 1% , 2%, and 3% of bulbs produced respectively by A, B, C are found to be defective. A bulb is picked up at random from the total production and found to be defective. Find the probability that this bulb was production by the machine A.

\*\*\*\*\* Best of luck \*\*\*\*\*