

# CLASS XI GUESS PAPER MATHS

## GURU NANAK ACADEMY SAFIDON

**Time: 3 hours**

**M.M. – 100**

- (i) All the questions are compulsory
- (ii) The Question paper consists of 29 questions.
- (iii) Questions 1 – 4 in Section A are very short answer type questions carrying 1 mark each.
- (iv) Questions 5 – 12 in Section B are short answer type questions carrying 2 marks each.
- (v) Questions 13 – 23 in Section C are long answer – I type questions carrying 4 marks each.
- (vi) Questions 24 – 29 in Section D are long answer type – II questions carrying 6 marks each.

### Section – A

1. Find the centre and radius of the circle  
 $x^2 + y^2 - 8y = 10y - 12 = 0$
2. Find the value of n such that  $n_{P_5} = 42 n_{P_3}$   $n > 4$
3. Solve  $\sqrt{5}x^2 + x + \sqrt{5} = 0$
4. Identify the type of “Or” used in the following statements and check whether the statements are true or false
  - (i)  $\sqrt{2}$  is a rational number or an irrational number.
  - (ii) To enter into a public library children need an identity card from the school or a letter from the school authorities.

### Section – B

5. Draw appropriate Venn diagram for each of following:
  - a.  $(A \cup B)^I$
  - b.  $(A \cap B)^I$
  - c.  $(A - B) \cup (B - A)$
  - d.  $A^I$
6. Prove that  $\sum_{r=0}^n 3^r \cdot {}^n C_r = 4^n$
7. Find the coordinates of the foci, the vertices, the length of major and minor axis of the ellipse  $9x^2 + 4y^2 = 36$

8. Show that the points P(-2, 3, 5), Q(1, 2, 3) and R(7, 0, -1) are collinear.

9. Evaluate:

a.  $\lim_{x \rightarrow 1} \left[ \frac{x^2+1}{x+100} \right]$

b.  $\lim_{x \rightarrow 1} \left[ \frac{x-2}{x^2-x} - \frac{1}{x^3-3x^2+2x} \right]$

10. Show that the statement

A: "If x is a real number such that  $x^3 + 4x = 0$ , then x is 0" is true by

- (a) Method of Contraction  
(b) Method of Contrapositive

11. A committee of two persons is selected from two men and two women. What is the probability that committee will have

- (a) no man?                      (b) one man?

12. If E and F are events such that  $P(E) = \frac{1}{4}$ ,  $P(F) = \frac{1}{2}$  and  $P(E \text{ and } F) = \frac{1}{8}$ , Find (a) P(E OR F)

- (b) P (not E and not F)

### Section – C

13. In a survey of 60 people it was found that 25 people read newspaper H, 26 read newspaper T, 26 read newspaper I, 9 read both H and I, 11 read both H and T, 8 read both T and I, 3 read all three newspapers. Find:

- (a) The number of people who read at least one of the newspapers.  
(b) The number of people who read exactly one newspaper.

14. Let  $A = \{1,2,3\}$ ,  $B = \{3,4\}$  and  $C = \{4,5,6\}$ . Find

- (a)  $A \times (B \cap C)$                       (c)  $A \times (B \cup C)$   
(b)  $(A \times B) \cap (A \times C)$                       (d)  $(A \times B) \cup (A \times C)$

15. Prove that  $\frac{\cos 4x + \cos 3x + \cos 2x}{\sin 4x + \sin 3x + \sin 2x} = \cot 3x$ .

16. Prove that  $1.2.3 + 2.3.4 + \dots + n.(n+1).(n+2) = \frac{n(n+1)(n+2)(n+3)}{4}$  for all  $n \in \mathbb{N}$ .

17. Convert  $Z = \frac{1+7i}{(2-i)^2}$  in the polar form.

18. Find the number of arrangements of the letters of the word INDEPENDENCE. In how many of these arrangements,

- a. do the words start with P.  
b. do all the vowels always occur together.  
c. do the vowels never occur together.

d. do the words begin with I and end in P?

19. Find a, if the 17<sup>th</sup> and 18<sup>th</sup> terms in the expansion of  $(2 + a)^{50}$  are equal.
20. If  $S_1, S_2$  and  $S_3$  are the sums of first n natural numbers, their square, their cubes respectively, show that  $9S_2^2 = S_3(1 + 8S_1)$ .
21. Find the equations of all the medians of the triangle ABC whose vertices are A(2, 5), B(-4, 9) and C(-2, -1)
22. Find the equation of the circle passing through the points (2,3) and (-1, 1) and whose centre is on the line  $x-3y-11=0$

**OR**

An arc is in the form of a parabola with its axis vertical. The arc is 10 m high and 5 m wide at the base. How wide is it 2 m from the vertex of the parabola.

23. Find the ratio in which the line joining the points (1, 2, 3) and (-3, 4, -5) is divided by the xy - plane. Also, find the coordinates of the point of division.

**OR**

Prove that the line joining the vertices of a tetrahedron to the centroids of the opposite faces are concurrent.

### Section – D

24. Prove that
- (a)  $\frac{(\sin 7x + \sin 5x) + (\sin 9x + \sin 3x)}{(\cos 7x + \cos 5x) + (\cos 9x + \cos 3x)} = \tan 6x$
- (b)  $(1 + \cot x - \operatorname{cosec} x)(1 + \tan x + \sec x) = 2$
25. Exhibit graphically the solution set of the linear in equations
- $$x + y \leq 5$$
- $$4x + y \geq 4$$
- $$x + 5y \geq 5$$
- $$x \leq 4$$
- $$x \leq 3$$

26. The sum of three numbers in G.P. is 56. If we subtract 1, 7, 21 from these numbers in that order, we obtain an arithmetic progression. Find the numbers.

**OR**

The sum of two numbers is 6 times their geometric mean, show that the numbers are in the ratio of  $(3+2\sqrt{2}) : (3 - 2\sqrt{2})$ .

27. Differentiate the following functions with respect to x.

(a)  $x^2 \sin x + \frac{1}{x^2}$

(b)  $\frac{ax^2+bx+c}{\sqrt{x}}$

(c)  $\left(\sqrt{x} + \frac{1}{\sqrt{x}}\right)^2$

**OR**

Evaluate:

$$\lim_{x \rightarrow 0} \frac{8}{x^8} \left[ 1 - \cos \frac{x^2}{2} - \cos \frac{x^2}{4} + \cos \frac{x^2}{4} + \cos \frac{x^2}{4} \right]$$

- 28.** Calculate the mean and standard deviation for the following table given the age distribution of a group of people:
- 29.** (a) The owner of a milk store finds that he can sell 980 litres of milk each week at Rs. 14/litre and 1220 litres of milk each week at Rs 16/litre. Assuming a linear relationship between selling price and demand, how many litres could he sell weekly at Rs 17/litre?
- (c) Find the angle between the lines  $y - \sqrt{3}x - 5 = 0$  and  $\sqrt{3}y - x + 6 = 0$ .