

CLASS X

SAMPLE PAPER

MATHS

Max.Marks: 80

Note: (i) This question paper consists of 40 questions divided into 4 sections A,B,C &D.

(ii) Questions in Section A carry 1 mark each, Section B carry 2 marks each, Section C carry 3 marks each and Section D carry 4 marks each.

(iii) There is no overall choice. However, internal choices are provided in 2 questions of Section A, 2 questions of Section B, 3 questions of Section C and 3 questions of Section D.

(iv) Use of calculators prohibited.

Section-A

- Decimal representation of $\frac{47}{4000}$ terminates after _____ digits.
a) 2 b) 3 c) 4 d) 5
- Square of a positive integer is always of the form ____
a) $3m$ b) $3m$ or $3m+1$ c) $3m + 1$ d) $3m$ or $3m + 2$
- If $\frac{5}{2}$ is a zero of the polynomial $4x^2 - 4x - k$, then value of 'k' is ____
a) 3 b) 15 c) - 15 d) 5
- The co-ordinates of the midpoint of the line joining points (4, -5) and (-6, 3) are____
a) (5,4) b) (-5, -4) c) (-1, -1) d) (1, 1)
- The distance between the points $(\cos\theta, \sin\theta)$ and $(\sin\theta, -\cos\theta)$ is ____
a) $\sqrt{3}$ b) $\sqrt{2}$ c) 2 d) 1
- If the distance between the points (4,p) and (1,0) is 5 units, then 'p' is ____
a) ± 4 b) 4 c) - 4 d) 0
- If $4\tan\theta = 3$, value of $\frac{4\sin\theta+3\cos\theta}{4\sin\theta-2\cos\theta}$ is ____
a) $5/3$ b) 6 c) - 6 d) Not defined.
- If $A + B = 90^\circ$ and $\cos B = \frac{3}{5}$, then $\sin A$ is ____
a) $\frac{3}{5}$ b) $\frac{4}{5}$ c) 1 d) none of these.
- If 5θ and 4θ are acute angles and $\sin 5\theta = \cos 4\theta$, then $2\sin 3\theta - \sqrt{3}\tan 3\theta$ is ____

- a) 1 b) -1 c) 0 d) $1+\sqrt{3}$
10. Twenty cards are numbered 1 – 20. One card is picked at random. The probability of card bearing a prime number is _____
- a) $\frac{2}{5}$ b) $\frac{3}{5}$ c) $\frac{1}{4}$ d) $\frac{7}{20}$

Questions (11-15) fill in the blanks:

11. The discriminant of the equation $\sqrt{3}x^2 + 2\sqrt{2}x - 2\sqrt{3} = 0$ is _____
12. Radius of a circle is do-ubled. Then the percent increase in its area is _____
13. Formula for finding Mode is _____ OR Formula for finding Median is _____
14. A circle is inscribed in a quadrilateral ABCD. Then $AB + DC =$ _____
15. Given $2x + 3y = 7$, An equation that would make the system of equations inconsistent is _____

Questions(16-20) Short answer questions.

16. If H.C.F of 45 and 63 can be expressed as $45m - 63X2$, then find 'm'.

OR

Find the largest number that divides 126, 144 and 198 completely.

17. For what value of 'k' the system of equations $2x + 3y = 5$; $4x - ky = 10$ will have infinitely many solutions.
18. For what value of 'k' the equation $x^2 - 8x + k = 0$ will have equal roots?
19. A tangent is drawn to a circle from a point 10 cm away from the centre is inclined at 30° to the line joining the point with the centre. Find the length of the tangent.
20. In ΔABC , $DE \parallel BC$. If $AB = 5$ cm, $AC = 7$ cm and $AD = 3$ cm find the length of EC.

Section-B

21. Draw a line segment $AB = 6$ cm and divide it in the ratio 3 : 2.

OR

Draw a circle of radius 2 cm and construct a tangent to it from a point on the circle.

22. Find the zeroes of the polynomial $4\sqrt{3}x^2 + 5x - 2\sqrt{3}$ and verify the relationship with the coefficients.

OR

If the squared difference between the zeroes of the polynomial $x^2 + px + 45$ is 144 find the value of 'p'.

23. Evaluate: $\frac{2}{3}(\cos^4\theta - \sin^4\theta) - 3(\sin^2 60^\circ - \sec^2 45^\circ) + \frac{1}{4}\cot^2 30^\circ$
24. AOB is the diameter of a circle with centre 'O'. AC and BC are two chords measuring 3 cm and 4 cm respectively. Find the area of the minor segments formed by chords AC and BC. ($\pi = 3.14$)
25. Find the mean of the following data by Direct method.

Class Int	0-10	10-20	20-30	30-40
Frequency	7	10	15	8

26. Two dice were tossed together. Find the probability of (i) both showing same score and (ii) sum of the scores is less than 6.

Section-C

27. Prove that $\sqrt{3}$ is irrational.

OR

Show that only one of 'n, n+1, n+2' is divisible by 3.

28. For what value of 'a' and 'b' the following system of equations will have infinitely many solutions. $2x - (2a+5)y = 5$; $(2b+1)x - 9y = 15$.
29. A lending library has fixed charge for the first three days and an additional charge thereafter. Savita pays ₹ 27 for a book kept for 7 days while Shriya paid ₹ 21 for a book kept for 5 days. Find the fixed charge and charge for extra day.
30. If the co-ordinates of the midpoints of a triangle are (1, 2), (0, - 1) and (2, - 1) find the co-ordinates of the vertices of the triangle.

OR

The vertices of a ΔABC are A(-2, 1), B(5, 4) and C (2, -3). Find the area of the triangle and the length of the altitude through A.

31. A circle is inscribed in a quadrilateral ABCD. Prove that the opposites sides subtend supplementary angles at the centre.
32. Two poles of height 'a' and 'b' meters are 'p' meters apart. Prove that the height of the intersection of lines joining the top of one pole with the foot of the other is given by $\frac{ab}{a+b}$ m.
33. Prove : $\frac{1+\cos\theta+\sin\theta}{1+\cos\theta-\sin\theta} = \frac{1+\sin\theta}{\cos\theta}$ OR $\frac{\tan^3\theta}{1+\tan^2\theta} + \frac{\cot^3\theta}{1+\cot^2\theta} = \sec\theta\csc\theta - 2\sin\theta\cos\theta$
34. ΔABC is right angled at B. With AC as diameter a semicircle is drawn and with BC as radius a quadrant is drawn. If AC = 5 cm and BC = 3cm find the area of the region between the semicircle and quadrant. ($\pi = 3.14$)

Section-D

35. Raju travels 600 km to his home partly by train and partly by car. If he travels 300 km by train and rest by car he would reach in 6 hours and 45 minutes, but if he travels 320 km by car rest by train he would take 3 minutes longer. Find the speeds of car and train.

OR

There are 20 coconut saplings planted in a row 10 m apart from each other. A gardener has to water these saplings one by one by fetching water from a well which is located 10 m away from first sapling. Find the distance covered in watering all plants and the time taken to complete the job if the speed of the gardener is 10 m /minute.

36. Find all zeroes of the polynomial $2x^4 - 2x^3 - 7x^2 + 3x + 6$ if two of the zeroes are $\sqrt{\frac{3}{2}}$ and $-\sqrt{\frac{3}{2}}$

37. If $\sin\theta - \cos\theta = \sqrt{2} \cos\theta$ prove that $\sin\theta + \cos\theta = \sqrt{2} \sin\theta$

OR

Angle of elevation of a jet flying horizontally at height of 3000m was found to be 45° . After a flight of ten seconds the angle of elevation changes to 60° . Find the speed of the jet. ($\sqrt{3} = 1.732$)

38. A cone of height 40 cm is cut horizontally by a plane parallel to the base. If the volume of the smaller cone so formed is $\frac{1}{64}$ of the original cone find at what height the section has been made.

OR

A solid is in the form of a cylinder with hemispherical ends. If the total height of the solid is 19 cm and diameter of the cylinder is 7 cm find the volume and total surface area.

39. $\triangle ABC$ is right angled at B and D and E are points on BC such that $BD = DE = EC$. Then prove that $8AE^2 = 5AD^2 + 3AC^2$.

40. If the median of the following data is 32.5 find the missing frequencies.

Class Int	0-10	10-20	20-30	30-40	40-50	50-60	60-70	Total
Freq	x	5	9	12	y	3	2	40