

CLASS X

SAMPLE PAPER

MATHS

Max. Marks: 80

Note: (i) This question paper consists of 40 questions divided into 4 sections A,B,C &D.

(ii) Questions in Section A carry 1 mark each, Section B carry 2 marks each, Section C carry 3 marks each and Section D carry 4 marks each.

(iii) There is no overall choice. However, internal choices are provided in 2 questions of Section A, 2 questions of Section B, 3 questions of Section C and 3 questions of Section D.

(iv) Use of calculators prohibited.

Section-A

- Given $\sqrt{2} = 1.41$, the value of $\sqrt{8}$ is ____
a) 2.14 b) 2.28 c) 2.82 d) 4.28
- Decimal representation of $\frac{117}{2500}$ terminates after ____ decimal digits.
a) 2 b) 3 c) 4 d) 5
- If 2 is a zero of the polynomial $x^3 - 6x^2 + px - 6$ the value of 'p' is ____
a) 11 b) -11 c) 12 d) -10
- The graph of the equation $4x - y = 8$ is intersected by the x-axis at ____
a) (2,0) b) (0,2) c) (-2, 0) d) (0, -2)
- The distance of the point (5,12) from the origin is ____ units.
a) 5 b)10 c) 13 d) 14
- If the points (2,5), (4, 6) and (x, 2) are collinear, then x = ____
a) 5 b) 6 c) 7 d) 8
- Probability of getting 53 Sundays in a leap year is ____
a) $\frac{1}{7}$ b) $\frac{2}{7}$ c) $\frac{3}{7}$ d) None of these
- If $\cot \theta = \frac{4}{3}$, $\operatorname{cosec}^2 \theta =$ ____
a) $\frac{5}{3}$ b) $\frac{25}{3}$ c) $\frac{25}{9}$ d) $\frac{9}{25}$
- Value of $\tan 85^\circ \sin 65^\circ \cos 0^\circ \sec 25^\circ \tan 5^\circ$ is ____
a) 0 b) 1 c) 4 d) None of these
- Length of the shadow of 6m high pole is $6\sqrt{3}$ m. The altitude of the Sun is ____

- a) 60° b) 30° c) 45° d) None of these

Q.11-15 (Fill in the Blanks)

11. If $3 + \sqrt{2}$ is one of the roots of the equation $ax^2 + bx + c = 0$, the other root is _____
 12. Length of arc of a circle of radius 8 cm is 12 cm. The area of the corresponding sector is _____
 13. _____ is the score that divides the given data into exactly two halves.
 14. Incircle of ΔABC touches the sides AB, BC and AC at D, E and F respectively. If $AD = 3.5$ cm, $BE = 2.6$ cm and $CF = 3$ cm The perimeter of the triangle is _____
 15. The division algorithm is _____

Q.16-20 (Short answer Questions)

16. Find the smallest number which when increased by 3 becomes divisible by 12, 15 and 18.

OR

Find the largest number that divides 64, 83 and 102 leaving remainders 1, 2 and 3 respectively.

17. In ΔABC D is a point on AC such that $\angle BDC = \angle ABC$. If $AC = 8$ cm, $CD = 2$ cm, Find the length of BC.
 18. In a right ΔABC having $\angle A = 90^\circ$, $AD \perp BC$. If $BD = 2$ cm and $CD = 8$ cm find the length of AD.
 19. For what value of 'k' the equation $2x^2 + kx + 2 = 0$ will have real roots?
 20. How many terms are there in the A.P. 6, 10, 14, 18, 174?

OR

Find the 15th term from the last of the A.P. 5, 12, 19, 250.

Section-B

21. Find the zeroes of the polynomial $9x^2 - 5\sqrt{6}x - 4$ and verify the relationship with the coefficients.

OR

Find the value of 'm' such that $(x - 5)$ is a factor of the polynomial $3x^3 - 16x^2 + mx + 50$

22. ABC is right triangle right angled at B. Prove that the perpendicular from B divides the triangle into two triangles similar each other and to original triangle.

23. Prove : $\frac{\tan(90^\circ - A)\cot A}{\operatorname{cosec}^2 A} - \cos^2 A = 0$

OR

Evaluate : $2(\cos^2 45^\circ + \tan^2 60^\circ) - 6(\sin^2 45^\circ - \tan^2 30^\circ)$

24. Find the area of a circular track of width 3.5 m and inner radius 21m.

25. From a well shuffled pack of cards find the probability of drawing a (i) face card (ii) a black card.
26. A bag contains 4 red, 3 blue and 9 red balls. How many green balls should be removed so that the difference between probability of drawing a green ball and probability of drawing a red ball is $\frac{1}{12}$.

Section-C

27. Given $\sqrt{2}$ and $\sqrt{3}$ are irrational prove $\sqrt{3} + \sqrt{2}$ is irrational.

OR

Prove that the cube of a positive integer is of the form $9m$, $9m + 1$ or $9m + 8$ for some integer m .

28. Solve for 'x' and 'y' : $73x + 29y = 380$: $29x + 73y = 28$

OR

Two stations are 60kms apart. Two cars start from these stations simultaneously. If they travel in the same direction they meet in 3 hours, but if they travel in opposite directions they meet in 20 minutes. Find the speeds of the cars.

29. A person saves Rs. 30 on 1st February 1996 and increases his savings every day by Rs.20. Find the amount saved by him in the month.
30. ABCD is a quadrilateral in which $AD = BC$. If P, Q, R and S are midpoints of AB, AC, DC and DB prove that PQRS is a rhombus.

OR

Side AC of $\triangle ABC$ is produced to D such that $CD = \frac{1}{2} AC$. If E is the midpoint of BC and DE produced meets AB at F, prove that $EF = \frac{1}{3} DF$.

31. In what ratio the joining points (12, 5) and (4, -3) is divided by the line $y = 2$. Find the coordinates of the point of division.
32. Construct a triangle ABC in which $AB = 4.5$ cm, $BC = 5$ cm and $\angle B = 45^\circ$, then construct a similar triangle to ABC with scale factor $\frac{4}{5}$.
33. Prove : $\frac{\cos^3 \theta + \sin^3 \theta}{\cos \theta + \sin \theta} + \frac{\cos^3 \theta - \sin^3 \theta}{\cos \theta - \sin \theta} = 2$
34. A trapezoid field has parallel sides measuring 70 m and 20 m. A horse is tethered at each corner of the field with a rope of length 3.5 m. Find the area not grazed by the horses if the perpendicular distance between the parallel sides is 28 m.

Section- D

35. Cost of a piece of cloth is Rs.400. Had the cloth been 4 m longer and the rate per meter been Rs. 5 less the cost would have remained same. Find the length of the cloth and rate per meter.

OR

If the remainder on division of $x^3 + 2x^2 + kx + 3$ by $(x - 3)$ is 21 Find the quotient and value of 'k'. Hence find the zeroes of the polynomial $x^3 + 2x^2 + kx - 18$

36. Water flows through a cylindrical pipe whose inner radius is 1 cm at the rate of 80cm/sec into an empty cylindrical tank of radius 40 cm. What will be the level of water in the tank after half an hour.

OR

A metallic right circular cone of height 20 cm and whose apical angle is 60° is cut into two parts at the middle of its height by a plane parallel to the base. If the frustum so obtained is drawn into a wire of diameter $\frac{1}{16}$ cm, find the length of the wire.

37. If the median of the following distribution is 28.5 find the missing frequencies.

Class Int	0-10	10-20	20-30	30-40	40-50	50-60	Total
Freq	5	x	20	15	y	5	60

OR

Draw a 'less than' type of ogive for the following data and obtain the median height from the graph. Verify the result by using the formula.

Wt(Kg)	<30	<40	<42	<44	<46	<48	<50	<52
No. of students	0	3	5	9	14	28	32	35

38. Two poles of equal height stand opposite to each other on either side of a 80 m wide road. From a point between them on the road the angles of elevation of their tops were found to be 60° and 30° respectively. Find the height of the poles and the distance of point from the poles.
39. In ΔABC , AD is the median on BC. Prove that $AB^2 + AC^2 = 2AD^2 + \frac{1}{2} BC^2$
40. The houses in a row are numbered consecutively 1 to 49. Find the house number such that sum of the house numbers preceding it is equal to the sum of the house numbers succeeding it.