

Time Allowed: 1 hour and 30 minutes

Maximum Marks: 40

General Instructions:

1. The question paper contains three parts A, B and C.
2. Section A consists of 20 questions of 1 mark each. Attempt any 16 questions.
3. Section B consists of 20 questions of 1 mark each. Attempt any 16 questions.
4. Section C consists of 10 questions based on two Case Studies. Attempt any 8 questions.
5. There is no negative marking.

Section A

Attempt any 16 questions

1. The decimal expansion of the number $\frac{441}{2^2 \times 5^3 \times 7^2}$ has [1]
 - a) None of these
 - b) non-terminating and non-repeating decimal
 - c) terminating decimal
 - d) non-terminating repeating decimal
2. The pair of equations $2x + 3y = 5$ and $4x + 6y = 15$ has [1]
 - a) infinitely many solutions
 - b) exactly two solutions
 - c) no solution
 - d) a unique solution
3. What should be subtracted to the polynomial $x^2 - 16x + 30$, so that 15 is the zero of the resulting polynomial? [1]
 - a) 15
 - b) 14
 - c) 16
 - d) 30
4. The solution of $\frac{a^2}{x} - \frac{b^2}{y} = 0$ and $\frac{a^2b}{x} + \frac{b^2a}{y} = a + b$ where $x, y \neq 0$ is [1]
 - a) $x = -a^2$ and $y = -b^2$
 - b) $x = a^2$ and $y = -b^2$
 - c) $x = a^2$ and $y = b^2$
 - d) $x = -a^2$ and $y = b^2$
5. If $\sin\theta - \cos\theta = 0$, then the value of $\sin^4\theta + \cos^4\theta$ is [1]
 - a) 1
 - b) $\frac{3}{4}$
 - c) $\frac{1}{4}$
 - d) $\frac{1}{2}$
6. $(2 + \sqrt{5})$ is [1]
 - a) an irrational number
 - b) not real number
 - c) a rational number
 - d) an integer

c) $x = -a^2$ and $y = -b^2$

d) $x = -a$ and $y = -b$

18. Two numbers 'a' and 'b' are selected successively without replacement in that order from the integers 1 to 10. The probability that $\frac{a}{b}$ is an integer, is **[1]**

a) $\frac{17}{45}$

b) $\frac{8}{45}$

c) $\frac{1}{5}$

d) $\frac{17}{90}$

19. The sum of a rational and an irrational number is **[1]**

a) Can be Rational or Irrational

b) Irrational

c) Always Rational

d) Rational

20. If A(5, 3), B(11, -5) and P(12, y) are the vertices of a right triangle right angled at P, then y = **[1]**

a) -1, 4

b) 2, 4

c) -2, 4

d) 2, -4

Section B

Attempt any 16 questions

21. In a cyclic quadrilateral ABCD, if $\angle A = (2x - 1)^\circ$, $\angle B = (y + 5)^\circ$, $\angle C = (2y + 15)^\circ$ and $\angle D = (4x - 7)^\circ$, then the value of $\angle C$ is **[1]**

a) 55°

b) 125°

c) 65°

d) 115°

22. A quadratic polynomial whose zeros are $\frac{3}{5}$ and $-\frac{1}{2}$, is **[1]**

a) $10x^2 - x + 3$

b) $10x^2 + x - 3$

c) $10x^2 - x - 3$

d) $10x^2 + x + 3$

23. If $a = 2^3 \times 3$, $b = 2 \times 3 \times 5$, $c = 3^n \times 5$ and $\text{LCM}(a, b, c) = 2^3 \times 3^2 \times 5$, then $n =$ **[1]**

a) 1

b) 4

c) 3

d) 2

24. $\cos^4 A - \sin^4 A$ is equal to **[1]**

a) $2 \sin^2 A - 1$

b) $2 \sin^2 A + 1$

c) $2 \cos^2 A + 1$

d) $2 \cos^2 A - 1$

25. The sum of the digits of a two digit number is 9. Nine times this number is twice the number obtained by reversing the digits, then the number is **[1]**

a) 72

b) 27

c) 18

d) 81

26. If α and β are the zeroes of the polynomial $x^2 - 6x + 8$, then the value of $\alpha^3 + \beta^3$ is **[1]**

a) 76

b) 72

c) 74

d) 80

27. Two poles of height 13 m and 7 m respectively stand vertically on a plane ground at a distance **[1]**

of 8 m from each other. The distance between their tops is

- a) 11 m
- b) 10 m
- c) 9 m
- d) 12 m

28. The ratio in which the point (1, 3) divides the line segment joining the points (-1, 7) and (4, -3) is

- a) 2 : 3
- b) 7 : 2
- c) 3 : 2
- d) 2 : 7

29. If $\tan \theta = \frac{1}{\sqrt{7}}$ then $\frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta} =$

- a) $\frac{1}{12}$
- b) $\frac{3}{7}$
- c) $\frac{3}{4}$
- d) $\frac{5}{7}$

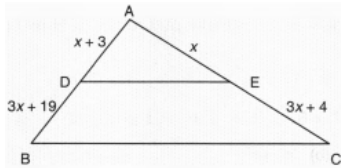
30. If $x = \alpha$ and $y = \beta$ is the solution of the equations $x - y = 2$ and $x + y = 4$, then

- a) $\alpha = 1$ and $\beta = 3$
- b) $\alpha = 3$ and $\beta = -1$
- c) $\alpha = 3$ and $\beta = 1$
- d) $\alpha = -3$ and $\beta = 1$

31. The exponent of 2 in the prime factorisation of 144, is

- a) 4
- b) 5
- c) 6
- d) 3

32. In the given figure value of x for which $DE \parallel BC$ is



- a) 3
- b) 2
- c) 4
- d) 1

33. If $\sin A + \sin^2 A = 1$, then the value of the expression $(\cos^2 A + \cos^4 A)$ is

- a) $\frac{1}{2}$
- b) 1
- c) 3
- d) 2

34. If the point $R(x, y)$ divides the join of $P(x_1, y_1)$ and $Q(x_2, y_2)$ internally in the given ratio $m_1 : m_2$, then the coordinates of the point R are

- a) $\left(\frac{m_2 x_1 - m_1 x_2}{m_1 + m_2}, \frac{m_2 y_1 - m_1 y_2}{m_1 + m_2}\right)$
- b) $\left(\frac{m_2 x_1 - m_1 x_2}{m_1 - m_2}, \frac{m_2 y_1 - m_1 y_2}{m_1 - m_2}\right)$
- c) $\left(\frac{m_2 x_1 + m_1 x_2}{m_1 + m_2}, \frac{m_2 y_1 + m_1 y_2}{m_1 + m_2}\right)$
- d) None of these

35. A child's game has 8 triangles of which 5 are blue and rest are red and 10 squares of which 6 are blue and the rest are red. One piece is lost at random. The probability that it is a square of blue colour is

- a) $\frac{4}{9}$
- b) $\frac{6}{10}$
- c) $\frac{1}{3}$
- d) $\frac{2}{3}$

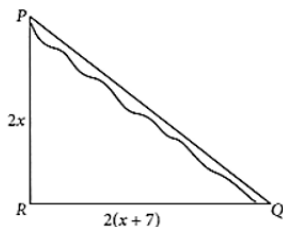
36. A system of linear equations is said to be consistent, if it has [1]
- a) two solutions b) one or many solutions
 c) no solution d) exactly one solution
37. $(1 + \sqrt{2}) + (1 - \sqrt{2})$ is [1]
- a) a rational number b) a non-terminating decimal
 c) None of these d) an irrational number
38. The value of $(\tan 1^\circ \tan 2^\circ \tan 3^\circ \dots \tan 89^\circ)$ is [1]
- a) 0 b) $\frac{1}{2}$
 c) 1 d) 2
39. If two different dice are rolled together, the probability of getting an even number [1]
- a) $\frac{1}{2}$ b) $\frac{1}{4}$
 c) $\frac{1}{36}$ d) $\frac{1}{6}$
40. If the endpoints of a diameter of a circle are $(-4, -3)$ and $(2, 7)$, then the coordinates of the centre are [1]
- a) $(1, -2)$ b) $(0, 0)$
 c) $(2, -1)$ d) $(-1, 2)$

Section C

Attempt any 8 questions

Question No. 41 to 45 are based on the given text. Read the text carefully and answer the questions:

Minister of a state went to city Q from city P. There is a route via city R such that $PR \perp RQ$. $PR = 2x$ km and $RQ = 2(x + 7)$ km. He noticed that there is a proposal to construct a 26 km highway which directly connects the two cities P and Q.

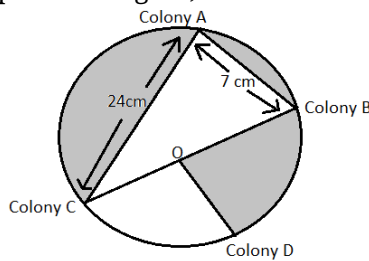


41. Which concept can be used to get the value of x ? [1]
- a) Converse of thales theorem b) Pythagoras theorem
 c) Thales theorem d) Converse of Pythagoras theorem
42. The value of x is [1]
- a) 5 b) 6
 c) 4 d) 8
43. The value of PR is [1]
- a) 20 km b) 25 km

- c) 10 km
 d) 15 km
44. The value of RQ is [1]
 a) 20 km
 b) 12 km
 c) 24 km
 d) 16 km
45. How much distance will be saved in reaching city Q after the construction of highway? [1]
 a) 4 km
 b) 9 km
 c) 8 km
 d) 10 km

Question No. 46 to 50 are based on the given text. Read the text carefully and answer the questions:

To find the polluted region in different areas of Dwarka (a part of Delhi represented by the circle given below) a survey was conducted by the students of class X. It was found that the shaded region is the polluted region, where O is the centre of the circle.



46. Find the radius of the circle. [1]
 a) 13.5 cm
 b) 12.5 cm
 c) 15 cm
 d) 16.5 cm
47. Find the area of the circle. [1]
 a) 495.6 cm²
 b) 491.07 cm²
 c) 481.7 cm²
 d) 490 cm²
48. If D lies at the middle of arc BC, then area of region COD is [1]
 a) 121 cm²
 b) 126 cm²
 c) 122.76 cm²
 d) 129.8 cm²
49. Area of the $\triangle BAC$ is [1]
 a) 81 cm²
 b) 79 cm²
 c) 84 cm²
 d) 77 cm²
50. Find the area of the polluted region. [1]
 a) 280.31 cm²
 b) 240.31 cm²
 c) 285.31 cm²
 d) 284.31 cm²



Solution

SAMPLE QUESTION PAPER AG-TMC-TS-P

Section A

1. (c) terminating decimal

Explanation: To check if the number is terminating: we will find the lowest form of the number.

$$\frac{441}{2^2 \times 5^7 \times 7^2}$$

$$\text{Here } 441 = 49 \times 9 = 7^2 \times 3^2$$

$$\frac{7^2 \times 3^2}{2^2 \times 5^7 \times 7^2} = \frac{3^2}{2^2 \times 5^7}$$

$$\text{Here denominator} = 2^2 \times 5^7$$

Here the denominator is of the form $2^m 5^n$

$$m = 2, n = 7$$

Hence, the number has a terminal decimal representation.

2. (c) no solution

Explanation: Here, $\frac{a_1}{a_2} = \frac{2}{4} = \frac{1}{2}$, $\frac{b_1}{b_2} = \frac{3}{6} = \frac{1}{2}$ and $\frac{c_1}{c_2} = \frac{-5}{-15} = \frac{1}{3}$

$$\therefore \frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$$

So, the given system has no solution.

3. (a) 15

Explanation:

We know that, if $x = \alpha$ is zero of a polynomial then $x - \alpha$ is a factor of $f(x)$

Since 15 is zero of the polynomial $f(x) = x^2 - 16x + 30$, therefore $(x - 15)$ is a factor of $f(x)$

Now, we divide $f(x) = x^2 - 16x + 30$ by $(x - 15)$ we get

$$\begin{array}{r} x-15 \overline{) x^2 - 16x + 30} \\ \underline{\pm x^2 \mp 15x} \\ -1x + 30 \\ \underline{\pm 1x \pm 15} \\ 15 \end{array}$$

Thus we should subtract the remainder 15 from $x^2 - 16x + 30$.

4. (c) $x = a^2$ and $y = b^2$

Explanation: First equation:

$$\frac{a^2}{x} - \frac{b^2}{y} = 0$$

$$\text{or } \frac{a^2}{x} = \frac{b^2}{y}$$

Second Equation:

$$\frac{a^2b}{x} + \frac{b^2a}{y} = a + b$$

$$\Rightarrow \left(\frac{b^2}{y}\right) \times b + \frac{b^2a}{y} = a + b$$

$$\Rightarrow \left(\frac{b^2}{y}\right) \times (b + a) = a + b$$

$$\Rightarrow \frac{b^2}{y} = \frac{a+b}{a+b} = 1$$

$$\Rightarrow y = b^2$$

$$\frac{a^2}{x} = \frac{b^2}{y}$$

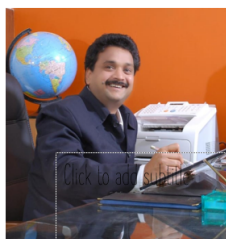
$$\Rightarrow \frac{a^2}{x} = \frac{b^2}{b^2} = 1$$

$$\Rightarrow x = a^2$$

Hence $x = a^2$ and $y = b^2$



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5. (d) $\frac{1}{2}$

Explanation: Given: $\sin \theta - \cos \theta = 0$
 $\Rightarrow \sin \theta = \cos \theta$
 $\Rightarrow \sin \theta = \sin(90^\circ - \theta)$
 $\Rightarrow \theta = 90^\circ - \theta \Rightarrow \theta = 45^\circ$
 $\therefore \sin^4 \theta + \cos^4 \theta = \sin^4 45^\circ + \cos^4 45^\circ$
 $= \left(\frac{1}{\sqrt{2}}\right)^4 + \left(\frac{1}{\sqrt{2}}\right)^4$
 $= \frac{1}{4} + \frac{1}{4}$
 $= \frac{1}{2}$

6. (a) an irrational number

Explanation: The sum of a rational and an irrational number is an irrational number hence it is an irrational number.

7. (b) $-\frac{3}{7}$

Explanation: Since α and β are the zeros of the quadratic polynomial $p(x) = 4x^2 + 3x + 7$

$$\alpha + \beta = \frac{-\text{Coefficient of } x}{\text{Coefficient of } x^2} = \frac{-3}{4}$$

$$\alpha\beta = \frac{\text{Constant term}}{\text{coefficient of } x^2} = \frac{7}{4}$$

$$\text{Now, } \frac{1}{\alpha} + \frac{1}{\beta} = \frac{\beta + \alpha}{\alpha\beta} = \frac{\frac{-3}{4}}{\frac{7}{4}} = \frac{-3}{4} \times \frac{4}{7} = \frac{-3}{7}$$

Thus, the value of $\frac{1}{\alpha} + \frac{1}{\beta}$ is $\frac{-3}{7}$.

8. (c) $\sqrt{85}$

Explanation: Let mid point of A(2, 2), B(-4, -4) be whose coordinates will be

$$= \left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right) = \left(\frac{2-4}{2}, \frac{2-4}{2}\right)$$

$$\text{or } \left(\frac{-2}{2}, \frac{-2}{2}\right) = (-1, -1)$$

\therefore Length of median CD

$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$= \sqrt{(5 + 1)^2 + (-8 + 1)^2}$$

$$= \sqrt{(6)^2 + (-7)^2} = \sqrt{36 + 49}$$

$$= \sqrt{85} \text{ units}$$

9. (a) 3

Explanation: The number of zeroes of a cubic polynomial is at most 3 because the highest power of the variable in cubic polynomial is 3, i.e. $ax^3 + bx^2 + cx + d$

10. (a) ± 3

Explanation: Let α, β are the zeroes of the given polynomial.

Given: $\alpha + \beta = \alpha\beta$

$$\Rightarrow \frac{-b}{a} = \frac{c}{a}$$

$$\Rightarrow -b = -c$$

$$\Rightarrow -(-27) = 3k^2$$

$$\Rightarrow k^2 = 9$$

$$\Rightarrow k = \pm 3$$

11. (c) $\frac{1}{2}$

Explanation: Prime number on a die are 2, 3, 5

$$\therefore \text{Probability of getting a prime number on the face of the die} = \frac{3}{6} = \frac{1}{2}$$

12. (d) 338

Explanation: HCF (26, 169) = 13

We have to find the value for LCM (26, 169)

We know that the product of numbers is equal to the product of their HCF and LCM.

Dr. AGYAT GUPTA MOB: 9425109601

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Therefore,

$$13(\text{LCM}) = 26(169)$$

$$\text{LCM} = \frac{26(169)}{13}$$

$$\text{LCM} = 338$$

13. (c) abscissa

Explanation: The distance of a point from the y-axis is the x (horizontal) coordinate of the point and is called abscissa.

14. (c) x-axis

Explanation: Since the ordinates of given points are 0. Therefore, points lie on x-axis.

15. (b) $-\frac{6}{5}$

Explanation: $x = 2$ satisfies $kx^2 + 3x + k = 0$

$$\therefore 4k + 6 + k = 0 \Rightarrow 5k = -6 \Rightarrow k = -\frac{6}{5}$$

16. (b) 9

Explanation: $9 \sec^2 A - 9 \tan^2 A$

$$= 9(\sec^2 A - \tan^2 A)$$

$$= 9(1) = 9$$

17. (a) $x = a$ and $y = b$

Explanation: Given

$$\frac{x}{a} + \frac{y}{b} = 2 \dots (i)$$

$$ax - by = a^2 - b^2 \dots (ii)$$

Eq (i) can be written as $bx + ay = 2ab \dots (iii)$

multiply equation (ii) by a and equation (iii) by b and adding

$$a^2 x + b^2 x = a^3 - ab^2 + 2ab^2 = a(a^2 + b^2)$$

$$x = a$$

multiply equation (ii) by b and equation (iii) by a and Subtract

$$-b^2 y - a^2 y = ba^2 - b^3 - 2ba^2$$

$$-y(b^2 + a^2) = -b(b^2 + a^2)$$

$$y = b$$

18. (d) $\frac{17}{90}$

Explanation: a and b are two number to be selected from the integers = 1 to 10 without replacement of a and b

i.e., 1 to 10 = 10

and 2 to 10 = 9

No. of ways = $10 \times 9 = 90$

Probability of $\frac{a}{b}$ where it is an integer

\therefore Possible event will be

= (2, 2), (3, 3), (4, 2), (4, 4), (5, 5), (6, 2), (6, 6), (7, 7), (8, 2), (8, 8), (9, 3), (9, 9), (10, 2), (10, 5)

(10, 10), = 17

$$P(E) = \frac{m}{n} = \frac{17}{90}$$

19. (b) Irrational

Explanation: Let rational number + irrational number = rational number

And we know " rational number can be expressed in the form of PQ, where p, q are any integers,

So, we can express our assumption As :

$$PQ + x = ab \text{ (Here x is a irrational number)}$$

$$x = ab - PQ$$

So,

x is a rational number, but that contradicts our starting assumption.

Hence rational number + irrational number = irrational number



20. (d) 2, -4

Explanation: A(5, 3), B(11, -5) and P(12, y) are the vertices of a right triangle, right-angled at P

$$\therefore AB^2 = (x_2 - x_1)^2 + (y_2 - y_1)^2 \text{ [BY P.G.T]}$$

$$= (11 - 5)^2 + (-5 - 3)^2 = (6)^2 + (-8)^2$$

$$= 36 + 64 = 100$$

$$\text{Similarly } BP^2 = (12 - 11)^2 + (y + 5)^2 = (1)^2 + y^2 + 10y + 25$$

$$= y^2 + 10y + 26$$

$$\text{and } AP^2 = (12 - 5)^2 + (y - 3)^2 = (7)^2 + (y - 3)^2$$

$$= 49 + y^2 - 6y + 8 = y^2 - 6y + 58$$

$\therefore \triangle ABP$ is a right triangle

$$\therefore AB^2 = BP^2 + AP^2$$

$$100 = y^2 + 10y + 26 + y^2 - 6y + 58$$

$$100 = 2y^2 + 4y + 84$$

$$\Rightarrow 2y^2 + 4y + 84 - 100 = 0 \Rightarrow 2y^2 + 4y - 16 = 0$$

$$\Rightarrow y^2 + 2y - 8 = 0 \text{ (Dividing by 2)}$$

$$\Rightarrow y^2 + 4y - 2y - 8 = 0 \left\{ \begin{array}{l} \because -8 = 4 \times (-2) \\ 2 = 4 - 2 \end{array} \right\}$$

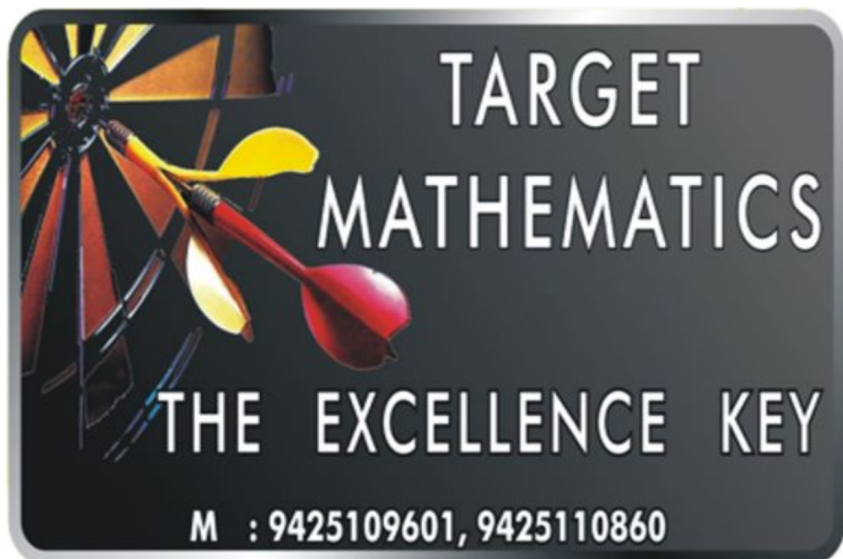
$$\Rightarrow y(y + 4) - 2(y + 4) = 0$$

$$\Rightarrow (y + 4)(y - 2) = 0$$

Either $y + 4 = 0$, then $y = -4$

or $y - 2 = 0$, then $y = 2$

$$y = 2, -4$$



Section B

21. (d) 115°

Explanation: Since the sum of the opposite angles of a cyclic quadrilateral is 180°

$$\therefore \angle A + \angle C = 180^\circ$$

$$\Rightarrow 2x - 1 + 2y + 15 = 180^\circ$$

$$\Rightarrow x + y = 83^\circ \dots (i)$$

And $\angle B + \angle D = 180^\circ$

$$\Rightarrow y + 5 + 4x - 7 = 180^\circ$$

$$\Rightarrow 4x + y = 182^\circ \dots (ii)$$

Subtracting eq. (ii) from eq. (i),

$$\text{we get } -3x = -99^\circ$$

$$\Rightarrow x = 33^\circ$$

Putting the value of x in eq. (i),

$$\text{we get } 33^\circ + y = 83^\circ$$

$$\Rightarrow y = 50^\circ$$

$$\therefore \angle C = (2y + 15)^\circ = (2 \times 50 + 15)^\circ = 115^\circ$$

22. (c) $10x^2 - x - 3$

$$\text{Explanation: } \alpha + \beta = \left(\frac{3}{5} - \frac{1}{2}\right) = \frac{1}{10}, \alpha\beta = \frac{3}{5} \times \left(\frac{-1}{2}\right) = \frac{-3}{10}$$

Required polynomial is $x^2 - \frac{1}{10}x - \frac{3}{10}$, i.e., $10x^2 - x - 3$

23. (d) 2

$$\text{Explanation: } \text{LCM}(a, b, c) = 2^3 \times 3^2 \times 5 \dots (I)$$

we have to find the value of n

Also we have

$$a = 2^3 \times 3$$

$$b = 2 \times 3 \times 5$$

$$c = 3^n \times 5$$

We know that while evaluating LCM, we take greater exponent of the prime numbers in the factorisation of the number.

Therefore, by applying this rule and taking $n \geq 1$ we get the LCM as

$$\text{LCM}(a, b, c) = 2^3 \times 3^n \times 5 \dots \text{(II)}$$

On comparing (I) and (II) sides, we get:

$$2^3 \times 3^2 \times 5 = 2^3 \times 3^n \times 5$$

$$n = 2$$

24. **(d)** $2 \cos^2 A - 1$

Explanation: We have, $\cos^4 A - \sin^4 A = (\cos^2 A + \sin^2 A)(\cos^2 A - \sin^2 A)$

$$= 1(\cos^2 A - \sin^2 A) = \cos^2 A - (1 - \cos^2 A)$$

$$= \cos^2 A - 1 + \cos^2 A$$

$$= 2 \cos^2 A - 1$$

25. **(c)** 18

Explanation: Let unit digit = x , Tens digit = y , therefore original no will be $10y + x$

Sum of digits are 9 So that $x + y = 9 \dots$ (i)

nine times this number is twice the number obtained by reversing the order of the digits $9(10y + x) = 2(10x + y)$

$$90y + 9x = 20x + 2y$$

$$88y - 11x = 0$$

Divide by 11 we get $8y - x = 0 \dots$ (ii)

Adding equations (i) and (ii), we get

$$9y = 9$$

$$y = \frac{9}{9} = 1$$

Putting this value in equation 1 we get

$$x + y = 9$$

$$x + 1 = 9$$

$$x = 8$$

Therefore the number is $10(1) + 8 = 18$

26. **(b)** 72

Explanation: Here $a = 1, b = -6, c = 8$

$$\text{Since } \alpha^3 + \beta^3 = (\alpha + \beta) [\alpha^2 + \beta^2 - \alpha\beta] = (\alpha + \beta) [(\alpha + \beta)^2 - 2\alpha\beta - \alpha\beta]$$

$$= (\alpha + \beta) [(\alpha + \beta)^2 - 3\alpha\beta]$$

$$= \left(\frac{-b}{a}\right) \left[\left(\frac{-b}{a}\right)^2 - 3 \times \frac{c}{a}\right]$$

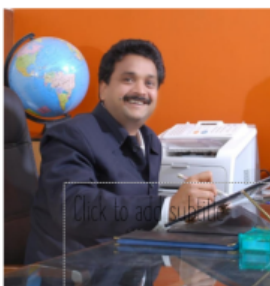
$$= \left(\frac{-b}{a}\right) \left[\frac{b^2}{a^2} - \frac{3c}{a}\right]$$

$$= \left(\frac{-b}{a}\right) \left[\frac{b^2 - 3ac}{a^2}\right]$$

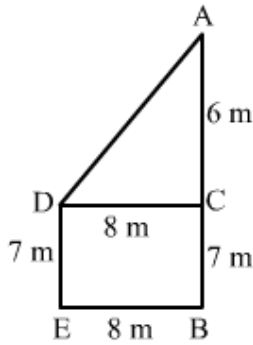
$$= \frac{-b^3 + 3abc}{a^3}$$

$$\text{Putting the values of } a, b \text{ and } c, \text{ we get } = \frac{-(-6)^3 + 3 \times 1 \times (-6) \times 8}{(1)^3} = \frac{216 - 144}{1} = 72$$

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27. (b) 10 m



Explanation:

Let AB and DE be the two poles.

According to the question:

$$AB = 13 \text{ m}$$

$$DE = 7 \text{ m}$$

$$\text{Distance between their bottoms} = BE = 8 \text{ m}$$

Draw a perpendicular DC to AB from D, meeting AB at C. We get:

$$DC = 8 \text{ m}, AC = 6 \text{ m}$$

Applying Pythagoras theorem in right-angled triangle ACD, we have:

$$AD^2 = DC^2 + AC^2 = 8^2 + 6^2 = 64 + 36 = 100$$

$$AD = \sqrt{100} = 10 \text{ m}$$

28. (a) 2 : 3

Explanation: Given: $(x, y) = (1, 3)$, $(x_1, y_1) = (-6, 10)$, $(x_2, y_2) = (3, -8)$

$$\text{Let } m_1 : m_2 = k : 1$$

$$\therefore x = \frac{m_1 x_2 + m_2 x_1}{m_1 + m_2}$$

$$1 = \frac{k \times 4 + 1 \times (-6)}{k + 1}$$

$$k + 1 = 4k - 6$$

$$\Rightarrow k = \frac{2}{3}$$

Therefore, the required ratio is 2 : 3

29. (c) $\frac{3}{4}$

$$\text{Explanation: } \tan \theta = \frac{1}{\sqrt{7}} = \frac{\text{Perpendicular}}{\text{Base}}$$

By Pythagoras Theorem,

$$(\text{Hyp.})^2 = (\text{Base})^2 + (\text{Perp.})^2$$

$$= (1)^2 + (\sqrt{7})^2 = 1 + 7 = 8$$

$$\therefore \text{Hyp.} = \sqrt{8} = 2\sqrt{2}$$

$$\text{Now, } \operatorname{cosec} \theta = \frac{\text{Hypotenuse}}{\text{Perpendicular}} = \frac{2\sqrt{2}}{1}$$

$$\sec \theta = \frac{\text{Hypotenuse}}{\text{Base}} = \frac{2\sqrt{2}}{\sqrt{7}}$$

$$\text{Now, } \frac{\operatorname{cosec}^2 \theta - \sec^2 \theta}{\operatorname{cosec}^2 \theta + \sec^2 \theta} = \frac{\left(\frac{2\sqrt{2}}{1}\right)^2 - \left(\frac{2\sqrt{2}}{\sqrt{7}}\right)^2}{\left(\frac{2\sqrt{2}}{1}\right)^2 + \left(\frac{2\sqrt{2}}{\sqrt{7}}\right)^2}$$

$$= \frac{8 - \frac{8}{7}}{8 + \frac{8}{7}}$$

$$= \frac{\frac{56-8}{7}}{\frac{56+8}{7}} = \frac{48}{64}$$

$$= \frac{48}{64} \times \frac{7}{7} = \frac{3}{4}$$

30. (c) $\alpha = 3$ and $\beta = 1$

Explanation: Given: $x - y = 2$... (i) ... (i)

And $x + y = 4$... (ii)

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Adding eq. (i) and (ii) for the elimination of y , we get

$$2x = 6$$

$$\Rightarrow x = 3$$

Putting the value of x in eq. (i), we get

$$3 - y = 2$$

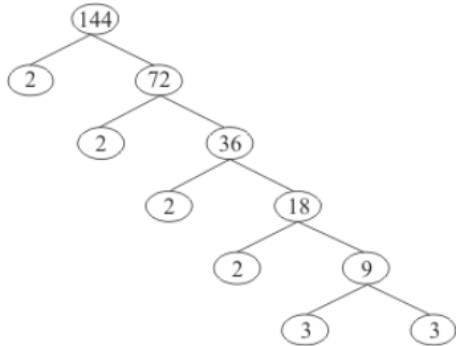
$$\Rightarrow y = 1$$

$$\therefore x = \alpha = 3 \text{ and } y = \beta = 1$$

31. (a) 4

Explanation:

Using the factor tree for prime factorisation, we have:



$$\text{Therefore, } 144 = 2 \times 2 \times 2 \times 2 \times 3 \times 3$$

$$\Rightarrow 144 = 2^4 \times 3^2$$

Thus, the exponent of 2 in 144 is 4.

32. (b) 2

Explanation: In $\triangle ABC$, $DE \parallel BC$

$$\therefore \frac{AD}{DB} = \frac{AE}{EC}$$

$$\Rightarrow \frac{x+3}{3x+19} = \frac{x}{3x+4}$$

$$\Rightarrow (x+3)(3x+4) = x(3x+19)$$

$$\Rightarrow 3x^2 + 4x + 9x + 12 = 3x^2 + 19x$$

$$\Rightarrow 3x^2 + 13x + 12 = 3x^2 + 19x$$

$$\Rightarrow 12 = 3x^2 + 19x - 3x^2 - 13x$$

$$\Rightarrow 12 = 6x \Rightarrow x = \frac{12}{6} = 2$$

$$\therefore x = 2$$

33. (b) 1

Explanation: Given that, $\sin A + \sin^2 A = 1$

$$\Rightarrow \sin A = 1 - \sin^2 A$$

$$\Rightarrow \sin A = \cos^2 A$$

$$\Rightarrow \sin^2 A = \cos^4 A$$

$$\Rightarrow 1 - \cos^2 A = \cos^4 A$$

$$\Rightarrow \cos^2 A + \cos^4 A = 1$$

34. (c) $\left(\frac{m_2x_1 + m_1x_2}{m_1 + m_2}, \frac{m_2y_1 + m_1y_2}{m_1 + m_2} \right)$

Explanation: If the point $R(x, y)$ divides the join of $P(x_1, y_2)$ and $Q(x_2, y_2)$

internally in the given ratio $m_1 : m_2$,

then the coordinates of the point R are $\left(\frac{m_2x_1 + m_1x_2}{m_1 + m_2}, \frac{m_2y_1 + m_1y_2}{m_1 + m_2} \right)$

35. (c) $\frac{1}{3}$

Explanation: Total number of pieces = 8 triangles + 10 squares = 18

Number of blue squares = 6

Number of possible outcomes = 6

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Number of total outcomes = $8 + 10 = 18$

$$\therefore \text{Required Probability} = \frac{6}{18} = \frac{1}{3}$$

36. **(b)** one or many solutions

Explanation: A system of linear equations is said to be consistent if it has at least one solution or can have many solutions. If a consistent system has an infinite number of solutions, it is dependent. When you graph the equations, both equations represent the same line. If a system has no solution, it is said to be inconsistent. The graphs of the lines do not intersect, so the graphs are parallel and there is no solution.

37. **(a)** a rational number

Explanation: $(1 + \sqrt{2}) + (1 - \sqrt{2}) = 1 + \sqrt{2} + 1 - \sqrt{2} = 1 + 1 = 2$ And 2 is a rational number. Therefore the given number is rational number.

38. **(c)** 1

Explanation: We have, $\tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 89^\circ$
 $= \tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 43^\circ \cdot \tan 44^\circ \cdot \tan 45^\circ \cdot \tan 46^\circ \cdot \tan 47^\circ \dots \tan 87^\circ \cdot \tan 88^\circ \cdot \tan 89^\circ$
 $= \tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 43^\circ \cdot \tan 44^\circ \cdot 1 \cdot \tan 46^\circ \cdot \tan 47^\circ \dots \tan 87^\circ \cdot \tan 88^\circ \cdot \tan 89^\circ$
($\because \tan 45^\circ = 1$)
 $= \tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 43^\circ \cdot \tan 44^\circ \cdot 1 \cdot \tan(90^\circ - 44^\circ) \cdot \tan(90^\circ - 43^\circ) \dots \tan(90^\circ - 3^\circ) \cdot \tan(90^\circ - 2^\circ) \cdot \tan(90^\circ - 1^\circ)$
 $= \tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 43^\circ \cdot \tan 44^\circ \cdot 1 \cdot \cot 44^\circ \cdot \cot 43^\circ \dots \cot 3^\circ \cdot \cot 2^\circ \cdot \cot 1^\circ$
($\because \tan(90^\circ - \theta) = \cot \theta$)
 $= \tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 43^\circ \cdot \tan 44^\circ \cdot 1 \cdot \frac{1}{\tan 44^\circ} \cdot \frac{1}{\tan 43^\circ} \dots \frac{1}{\tan 3^\circ} \cdot \frac{1}{\tan 2^\circ} \cdot \frac{1}{\tan 1^\circ}$
($\because \tan \theta = \frac{1}{\cot \theta}$)
 $= \left(\tan 1^\circ \times \frac{1}{\tan 1^\circ} \right) \cdot \left(\tan 2^\circ \times \frac{1}{\tan 2^\circ} \right) \dots \left(\tan 44^\circ \times \frac{1}{\tan 44^\circ} \right) = 1$
Hence, $\tan 1^\circ \cdot \tan 2^\circ \cdot \tan 3^\circ \dots \tan 89^\circ = 1$

39. **(b)** $\frac{1}{4}$

Explanation: Rolling two different dice, Number of total events = $6 \times 6 = 36$
Number of even number on both dice are $\{(2,2), (2,4), (2,6), (4,2), (4,4), (4,6), (6,2), (6,4), (6,6)\} = 9$
 $\therefore \text{Probability} = \frac{9}{36} = \frac{1}{4}$

40. **(d)** (-1, 2)

Explanation: Let the coordinates of centre O be (x, y).
The endpoints of a diameter of the circle are A(-4, -3) and B(2, 7).
Since centre is the midpoint of diameter.
 $\therefore x = \frac{x_1 + x_2}{2} = \frac{-4 + 2}{2} = \frac{-2}{2} = -1$ and
 $y = \frac{y_1 + y_2}{2} = \frac{-3 + 7}{2} = \frac{4}{2} = 2$
Therefore, the coordinates of the centre O is (-1, 2)

Section C

41. **(b)** Pythagoras theorem

Explanation: Pythagoras theorem

42. **(a)** 5

Explanation: Using Pythagoras theorem, we have

$$PQ^2 = PR^2 + RQ^2$$

$$\Rightarrow (26)^2 = (2x)^2 + (2(x + 7))^2 \Rightarrow 676 = 4x^2 + 4(x + 7)^2$$

$$\Rightarrow 169 = x^2 + x^2 + 49 + 14x \Rightarrow x^2 + 7x - 60 = 0$$

$$\Rightarrow x^2 + 12x - 5x - 60 = 0 \Rightarrow x(x + 12) - 5(x + 12) = 0 \Rightarrow (x - 5)(x + 12) = 0$$

$$\Rightarrow x = 5, x = -12$$

$\therefore x = 5$ [Since length can't be negative]

43. **(c)** 10 km

Explanation: $PR = 2x = 2 \times 5 = 10$ km

44. **(c)** 24 km

Explanation: $RQ = 2(x + 7) = 2(5 + 7) = 24$ km

45. (c) 8 km

Explanation: Since $PR + RQ = 10 + 24 = 34$ km
Saved distance = $34 - 26 = 8$ km

46. (b) 12.5 cm

Explanation: Since BOC is the diameter and $\angle BAC = 90^\circ$
 $\therefore BC^2 = AB^2 + AC^2$
 $= 7^2 + 24^2 = 625$
 $\Rightarrow BC = 25$ cm
 \therefore Radius of circle = $\frac{25}{2}$ cm = 12.5 cm

47. (b) 491.07 cm²

Explanation: Area of circle = $\pi(12.5)^2 = \frac{22}{7} \times 12.5 \times 12.5$
 $= 491.07$ cm²

48. (c) 122.76 cm²

Explanation: Clearly, $\angle COD = 90^\circ$ [$\because \angle COB = 180^\circ$ and equal arcs subtends equal angles at the centre]
Area of region COD = $\frac{90^\circ}{360^\circ} \times \pi r^2$
 $= \frac{1}{4}(491.07) = 122.76$ cm²

49. (c) 84 cm²

Explanation: Area of $\triangle BAC = \frac{1}{2} \times AB \times AC$
 $= \frac{1}{2} \times 7 \times 24 = 84$ cm²

50. (d) 284.31 cm²

Explanation: Area of the polluted region = Area of circle - Area of sector COD - Area of $\triangle ABC$
 $= 491.07 - 122.76 - 84$
 $= 284.31$ cm²

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