

## SQP-3-Term-2-Session-2021-22

06 March 2022 11:30 PM

### Sample Question Paper

**CLASS: XII**

**Session: 2021-22**

**Mathematics**

**Term - 2**

**Time Allowed: 2 hours**

**Maximum Marks: 40**

**General Instructions:**

1. This question paper contains **three sections - A, B and C**. Each part is compulsory.
2. **Section - A** has **6 short answer type (SA1)** questions of 2 marks each.
3. **Section B** has **4 short answer type (SA2)** questions of 3 marks each.
4. **Section - C** has **4 long answer type questions (LA)** of 4 marks each.
5. There is an **internal choice** in some of the questions.
6. Q14 is a **case-based problem** having 2 sub parts of 2 marks each.

### SECTION - A

1.	Find $\int \frac{xe^x}{(1+x)^2} dx$  OR  Find $\int_0^2 (x - [x]) \cdot dx$	2
2.	Write the sum of the order and the degree of the following differential equation: $\frac{d^2y}{dx^2} = \frac{3y + \frac{dy}{dx}}{\sqrt{\frac{d^2y}{dx^2}}}$	2
3.	If $\vec{p} = (2\hat{i} - 3\hat{j} - 6\hat{k})$ , Find the scalar and vector projections of $\vec{p}$ on the line joining the points $(3,4, -2)$ and $(5,6, -3)$ .	2
4.	Find the angle between the line $\frac{x+3}{2} = \frac{y-1}{1} = \frac{z+4}{-2}$ and the plane $x + y + 4 = 0$	2
5.	A couple has 3 children. Find the probability that they have at least one child of each gender ?	2
6.	An anti-aircraft gun fired three shots to a fighter plane. The probability of hitting the target by the first shots is 0.4; second shots is 0.5 and the third shot is 0.7. Find the probability that the target is destroyed.	2
<u>SECTION B</u>		
7.	Find: $\int e^x \left( \frac{1 + \sin x}{1 + \cos x} \right) dx$	3
8.	Find the particular solution of the following differential equation: $(2x + y + 1) dx + (4x + 2y - 1) dy = 0, y(0) = 1$  OR  Find the general solution of the differential equation: $(x + \tan y) dy = (\sin 2y) dx$	3

9.	If $\vec{a}$ , $\vec{b}$ , $\vec{c}$ are three mutually perpendicular unit vectors, find the angle inclined by $(\vec{a} + \vec{b} + \vec{c})$ with $\vec{a}$ , $\vec{b}$ and $\vec{c}$ .	3
10.	<p>Find the shortest distance between the following lines <math>\frac{x-3}{2} = \frac{y+15}{-7} = \frac{z-9}{5}</math>  and <math>\frac{x+1}{2} = \frac{y-1}{1} = \frac{z-9}{-3}</math>.</p> <p style="text-align: center;">OR</p> <p>Find the vector and cartesian equation of the plane(s) passes through the intersection of the planes, <math>x + 3y - z + 1 = 0</math> and <math>3x - y + 5z + 3 = 0</math> and are at a distance <math>\frac{2}{3}</math> units from origin .</p>	3
<u>SECTION C</u>		
11.	Evaluate: $\int_0^1 \left\{ \frac{\log(1+x)}{1+x^2} \right\} dx$	4
12.	<p>Using integration, Find the area of the region into which the circle <math>x^2 + y^2 = 4</math> is divided by the line <math>x + \sqrt{3}y = 2</math>.</p> <p style="text-align: center;">OR</p> <p>Using integration, determine the area common to the parabola <math>y^2 = x</math> and the circle <math>x^2 + y^2 = 2x</math></p>	4
13.	Find the foot of the perpendicular drawn from the point (5,7,3) to the line: $\frac{x-15}{3} = \frac{y-29}{8} = \frac{z-5}{-5}$ Find the length of the perpendicular and its equation.	4
14.	<p style="text-align: center;"><b><u>CASE-BASED/DATA-BASED</u></b></p>  <p>From a survey conducted in a cancer hospital it is found that 10% of the patients were alcoholics, 30% chew gutka and 40% have no specific carcinogenic habits. If cancer strikes 80% of the smokers, 70% of alcoholics, 50% of gutka chewers and 10% of the non-specific, then given that no patient has more than one bad habits, estimate the probability that</p> <p><b>Based on the given information, answer the following questions.</b></p>	
	(i) A patient is chosen at random from smokers or alcoholics group. What is the probability that the selected person be affected with cancer ?	2
	(ii) A cancer patient chosen from any one of the above types, selected at random, has no specific carcinogenic habits ?	2

