



# Modern Middle East International School

Academic Year 2021 – 2022

## PREBOARD EXAMINATION -3

<b>Name:</b>	<b>Subject: Mathematics - STANDARD</b>	<b>Date: 10-4-2022</b>
<b>Class: 10</b>	<b>Set: A</b>	<b>Duration: 2 hours</b>
<b>Section:</b>	<b>Max. Marks: 40</b>	<b>Marks Obtained:</b>

### General Instructions:

1. The question paper consists of 14 questions divided into 3 sections A, B, C.
2. All questions are compulsory.
3. Section A comprises of 6 questions of 2 marks each. Internal choice has been provided in two questions.
4. Section B comprises of 4 questions of 3 marks each. Internal choice has been provided in one question.
5. Section C comprises of 4 questions of 4 marks each. An internal choice has been provided in one question. It contains two case study based questions.

### SECTION-A

[6 x 2 = 12M]

- 1) Find  $k$  so that the quadratic equation  $(k + 1)x^2 - 2(k + 1)x + 1 = 0$  has equal roots.
- 2) Find the nature of the roots of the quadratic equation  $3x^2 - 4\sqrt{3}x + 4 = 0$  and hence solve it.

(OR)

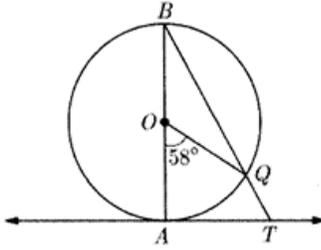
A two digit number is four times the sum of the digits. It is also equal to 3 times the product of the digits. Find the number.

- 3) Find the middle term of the A.P 213, 205, 197, ...37.

(OR)

Find the number of natural numbers between 102 and 998 which are divisible by 2 and 5 both.

- 4) In the given figure, AB is the diameter of a circle with center O and AT is the tangent. If  $\angle AOQ = 58^\circ$ , find  $\angle ATQ$ .



- 5) A solid metallic sphere of radius 10.5 cm is melted and recast into a number of smaller cones, each of radius 3.5cm and height 3cm. Find the number of cones so formed.
- 6) The following table shows the cumulative frequency distribution of marks of 80 students in an examination:

Marks	Number of students
Below 10	1
Below 20	5
Below 30	13
Below 40	27
Below 50	44
Below 60	57
Below 70	67
Below 80	74
Below 90	78
Below 100	80

Construct a frequency distribution table for the data above.

### **SECTION-B**

[ 3 x 4 = 12M ]

- 7) The maximum bowling speeds, in km per hour, of 33 players at a cricket coaching center are given as follows :

Speed (km/h)	85-100	100-115	115-130	130-145
Number of players	11	9	8	5

Calculate the median bowling speed.

8) The daily income of a sample of 50 employees are tabulated as follows:

Income (in Rs)	1-200	201-400	401-600	601-800
Number of employees	14	15	14	7

Find the mean daily income of employees.

9) Draw a circle of radius 4 cm. Construct a pair of tangents to it, the angle between which is  $60^\circ$ . Also justify the construction. Measure the distance between the center of the circle and the point of intersection of tangents.

10) Amit, standing on a horizontal plane, finds a bird flying at a distance of 200 m from him at an elevation of  $30^\circ$ . Deepak standing on the roof of a 50 m high building, finds the angle of elevation of the same bird to be  $45^\circ$ . Amit and Deepak are on opposite sides of the bird. Find the distance of the bird from Deepak.

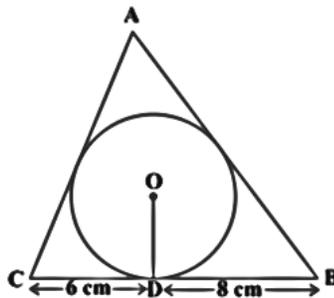
**(OR)**

The shadow of a tower standing on a level plane is found to be 50 m longer when Sun's elevation is  $30^\circ$  than when it is  $60^\circ$ . Find the height of the tower.

**SECTION-C**

**[4 x 4 = 16M ]**

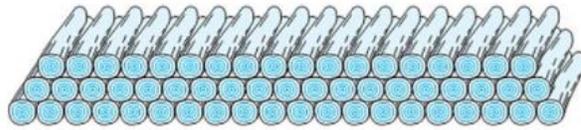
11) A triangle ABC is drawn to circumscribe a circle of radius 4 cm such that the segments BD and DC into which BC is divided by the point of contact D are of lengths 8 cm and 6 cm respectively as shown in the figure given below. Find the sides AB and AC.



12) A man rowing a boat away from a lighthouse 100 m high takes 2 minutes to change the angle of elevation of the top of lighthouse from  $60^\circ$  to  $30^\circ$ . Find the speed of the boat in metres per min. [Use  $\sqrt{3} = 1.732$  ]

**Case Study-1**

13) 200 logs are stacked in the following manner: 20 logs in the bottom row, 19 in the next row, 18 in the row next to it and so on as shown in the figure.

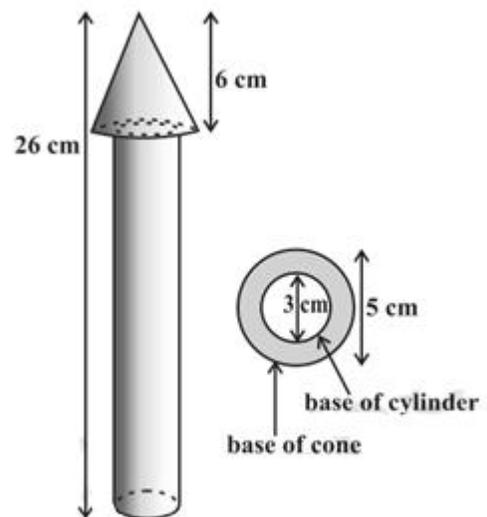


- i) In how many rows are the 200 logs placed.
- ii) How many logs are in the top row?

### Case Study-2

14). A wooden toy rocket is in the shape of a cone mounted on a cylinder, as shown in the figure. The height of the entire rocket is 26 cm, while the height of the conical part is 6 cm. The base of the conical portion has a diameter of 5 cm, while the base diameter of the cylindrical portion is 3 cm. The conical portion is to be painted orange and the cylindrical portion yellow (Take  $\pi = 3.14$ )

- i) Find the area of the rocket to be painted orange color.
- ii). Find the area of the rocket to be painted yellow color.



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