



PRAGATHI...THE SCHOOL

Dakshina Bharatha Mahila Samaja Premises,
Whitefield Railway Station Road, Kadugodi, Bangalore - 560067

Date : 26/11/2022

Periodic Test - 1

Time allowed : 3Hrs

MATHEMATICS(Standard) - 041

Maximum Marks: 80

General instructions:

1. This Question Paper has 5 **Sections A-E**.
2. Section **A** has **20** MCQs carrying **1** mark each
3. Section **B** has **5** questions carrying **02** marks each.
4. Section **C** has **6** questions carrying **03** marks each.
5. Section **D** has **4** questions carrying **05** marks each.
6. Section **E** has **3** case based integrated units of assessment (**04** marks each) with sub-parts of the values of **1, 1** and **2** marks each respectively.
7. All Questions are compulsory. However, an internal choice in **2** Qs of **5** marks, **2** Qs of **3** marks and **2** Questions of **2** marks has been provided. An internal choice has been provided in the **2** marks questions of Section E
8. Draw neat figures wherever required. Take $\pi = 22/7$ wherever required if not stated.

Section A consists of 20 questions of 1 mark each.

1. Let a and b be two positive integers such that $a = p^3q^4$ & $b = p^2q^3$, where p and q are prime numbers. If $HCF(a,b) = p^m q^n$ and $LCM(a,b) = p^r q^s$, then $(m+n)(r+s) =$
(a) 15 (b) 30 (c) 35 (d) 72
2. The number $(\sqrt{3} + \sqrt{5})^2$ is
a) an irrational number (b) an integer
c) a rational number (d) not a real number
3. Let p be a prime number. The quadratic equation having its roots as factors of p is
(a) $x^2 - px + p = 0$ (b) $x^2 - (p+1)x + p = 0$ (c) $x^2 + (p+1)x + p = 0$ (d) $x^2 - px + p + 1 = 0$
4. If the sum and product of the roots of the equation $kx^2 + 6x + 4k = 0$ are equal, then $k =$
(a) $3/2$ (b) $-2/3$ (c) $-3/2$ (d) $2/3$
5. The HCF of two consecutive even numbers is
a) 2 (b) 1 (c) 0 (d) 3
6. The distance between the points $(3, -2)$ and $(-3, 2)$ is:
a) 40 (b) $4\sqrt{10}$ (c) $2\sqrt{10}$ (d) $\sqrt{52}$
7. If the vertices of a parallelogram PQRS taken in order are $P(3,4)$, $Q(-2,3)$ and $R(-3,-2)$, then the coordinates of its fourth vertex S are
(a) $(-2,-1)$ (b) $(-2,-3)$ (c) $(2,-1)$ (d) $(1,2)$
8. ABCD is a trapezium with $AD \parallel BC$ and $AD = 4\text{cm}$. If the diagonals AC and BD intersect each other at O such that $AO/OC = DO/OB = 1/2$, then $BC =$
a) 6cm (b) 7cm (c) 8cm (d) 9cm

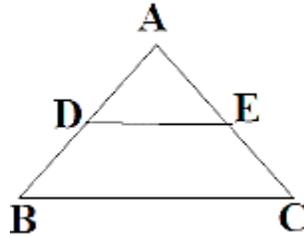
9. In the given figure $DE \parallel BC$, $AE = a$ units, $EC = b$ units $DE = x$ units $BC = y$ units, which of the following is true?

(a) $x = \frac{a+b}{ay}$

(b) $y = \frac{ax}{a+b}$

(c) $x = \frac{ay}{a+b}$

(d) $\frac{x}{y} = \frac{a}{b}$



10. If two tangents inclined at an angle of 60° are drawn to a circle of radius 3cm, then the length of each tangent is equal to

a) $3\sqrt{3}$ cm

b) 3cm

c) 6cm

d) $\frac{\sqrt{3}}{3}$ cm

11. The area of a circle that can be inscribed in a square of 6cm is

a) 36π cm²

b) 18π cm²

c) 12π cm²

d) 9π cm²

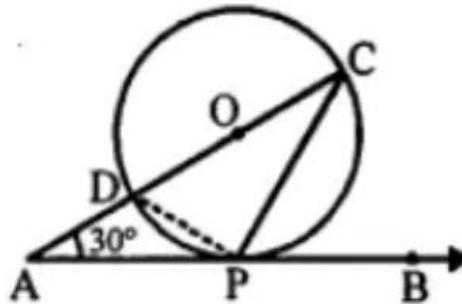
12. In the given figure, O is the centre of the circle. AB is the tangent to the circle at the point P. If $\angle PAO = 30^\circ$ then $\angle CPB + \angle ACP$ is equal to

a) 120°

b) 90°

c) 150°

d) 60°



13. One ticket is drawn at random from a bag containing tickets numbered 1 to 40. The probability that the selected ticket has a number, which is a multiple of 7, is

a) $1/5$

b) $1/8$

c) $1/7$

d) $7/40$

14. The difference of mode and median of a data is 24, then the difference of median and mean of the data is

a) 8

b) 12

c) 24

d) 36

15. The mean of 20 numbers is zero. Of them, at the most, how many may be greater than zero?

a) 1

b) 0

c) 10

d) 19

16. A bag contains 3 red balls, 5 white balls and 7 black balls. What is the probability that a ball drawn from the bag at random will be neither red nor black?

a) $1/3$

b) $8/15$

c) $7/15$

d) $1/5$

17. Two dice are thrown simultaneously. The probability that the sum of the numbers appearing on the dice is 1 is

a) 3

b) 0

c) 2

d) 1

18. In a lottery , there are 8 prizes and 16 blanks. What is the probability of getting a prize?

- a) $1/2$ b) $1/3$ c) $2/3$ d) None of these

19. **Assertion (A):** L.C.M. and H.C.F . of a and 20 are 100 and 10 respectively , then $a = 50$.

Reason (R): L.C.M H.C.F . = First number X Second number

- a) Both A and R are true and R is the correct explanation of A.
b) Both A and R are true but R is not the correct explanation of A.
c) A is true but R is false. d) A is false but R is true.

20. **Assertion (A):** In a circle of radius 6 cm, the angle of a sector is 60° . Then the area of the sector is $132/7 \text{ cm}^2$

Reason (R): Area of the circle with radius r is πr^2 .

- a) Both A and R are true and R is the correct explanation of A.
b) Both A and R are true but R is not the correct explanation of A.
c) A is true but R is false. d) A is false but R is true.

Section B consists of 5 questions of 2 marks each.

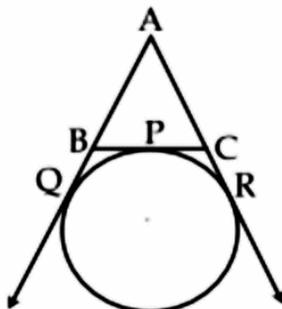
21. Find the zeroes of the quadratic polynomial $2x^2 - 25$.

22. If the point $A(0, 2)$ is equidistant from the points $B(3, p)$ and $C(p, 5)$, find p . Also find the length of AB .

OR

In what ratio does the point $P(2, -5)$ divide the line segment joining $A(-3, 5)$ and $B(4, -9)$?

23. In fig. circle touches the side BC of a triangle ABC at the point P and AB and AC produced at Q and R . Show that $AQ = 1/2$ (perimeter $\triangle ABC$)



OR

Prove that tangents drawn at the ends of a chord make equal angles with the chord

24. A chord of circle of radius 10cm subtends a right angle at the centre. Find the area of the minor segment.

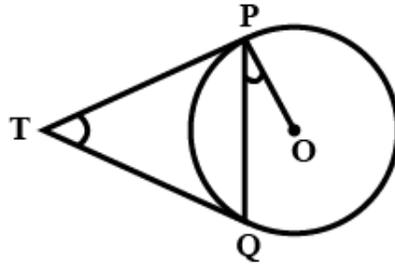
25. The probability of selecting a blue marble at random from a jar that contains only blue, black and green marbles is $1/5$. The probability of selecting a black marble at random from the same jar is $1/4$. If the jar contains 11 green marbles, find the total number of marbles in the jar.

Section C consists of 6 questions of 3 marks each.

26. Prove that $\sqrt{3}$ is an irrational number.

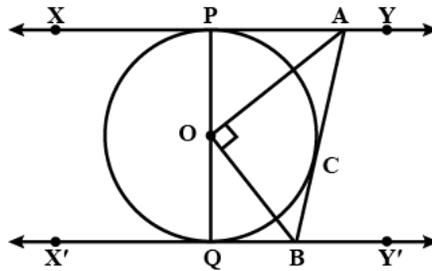
27. Find the zeroes of the following quadratic polynomials $6x^2 - 3 - 7x$ and verify the relationship between the zeros and the coefficients.

28. Two tangent TP and TQ are drawn to a circle with centre O from an external point T. Prove that $\angle PTQ = 2 \angle OPQ$

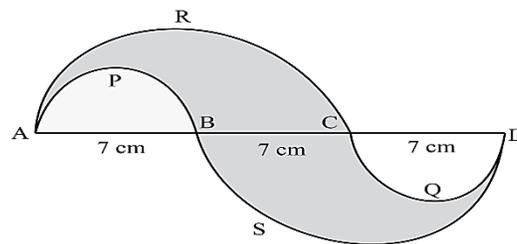


OR

In the figure XY and X'Y' are two parallel tangents to a circle with centre O and another tangent AB with point of contact C intersecting XY at A and X'Y' at B prove that $\angle AOB = 90^\circ$

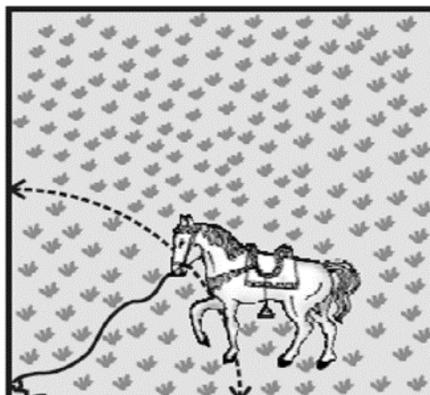


29. In the given fig, APB and CQD are semi circles of diameter 7 cm each, while ARC and BSD are semicircles of diameter 14 cm each. Find the perimeter & Area of the shaded region. (Use $\pi = 22/7$)

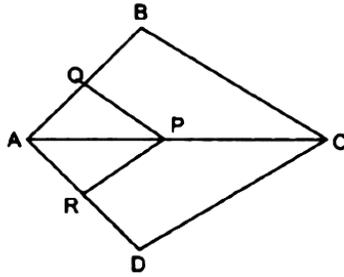


OR

A horse is tied to a peg at one corner of a square shaped grass field of side 15 m by means of a 5 m long rope . Find (i) the area of that part of the field in which the horse can graze. (ii) the increase in the grazing area if the rope were 10 m long instead of 5 m.



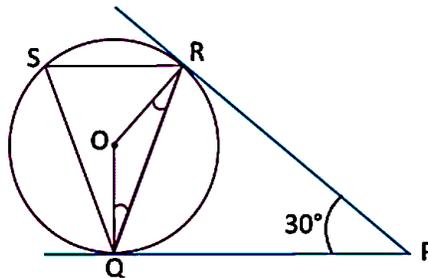
30. If $PQ \parallel BC$ & $PR \parallel CD$. Prove that (i) $\frac{AR}{AD} = \frac{AQ}{AB}$ (ii) $\frac{QB}{AQ} = \frac{DR}{AR}$



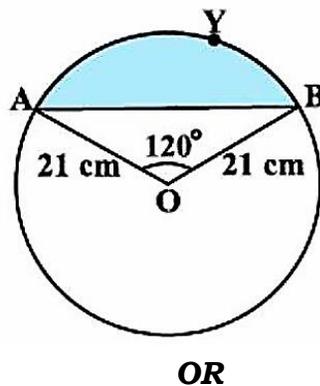
31. Cards marked with the number 2 to 101 are placed in a box and mixed thoroughly. One card is drawn from the box. Find the probability that the number on the card is:
- (i) A number is perfect square
 - (ii) A prime number less than 20
 - (iii) A composite number less than 30

Section D consists of 4 questions of 5 marks each.

32. Prove that if a line is drawn parallel to one side of a triangle intersecting the other two sides in distinct points, then the other two sides are divided in the same ratio.
Using the above theorem prove that a line through the point of intersection of the diagonals and parallel to the base of the trapezium divides the non parallel sides in the same ratio.
33. In the given figure, Find $\angle ROQ$, $\angle RQP$, $\angle RSQ$ & $\angle ORP$. If $PQ=40m$ and $OQ=30m$ then $PO=$



34. Find the area of the segment AYB shown in Fig., if radius of the circle is 21 cm and $\angle AOB = 120^\circ$. (Use $\pi = 22/7$)



Prove that opposite sides of a quadrilateral circumscribing a circle subtend supplementary angles at the centre of the circle

35. If the median of the distribution given below is 28.5, find the values of x and y .

Class	0-10	10-20	20-30	30-40	40-50	50-60	Total
Frequency	5	x	20	15	y	5	60

OR

The median of the following data is 525. Find the values of x and y , if the total frequency is 100

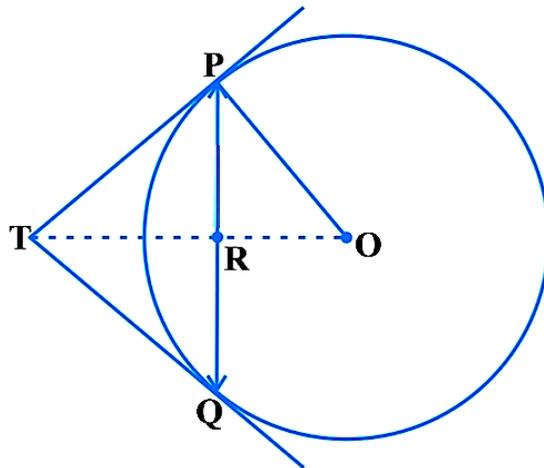
Class interval	Frequency
0-100	2
100-200	5
200-300	x
300-400	12
400-500	17
500-600	20
600-700	y
700-800	9
800-900	7
900-1000	4

Section E Case study-based questions are compulsory.

Consists of 3 questions of 4 marks each.

36. Case Study – 1

PQ is a chord of length 24 cm of a circle of radius 13 cm. The tangents at P and Q intersect at a point T .



- 1) Find OR
- 2) Find TR
- 3) Find TP

OR

Find QT

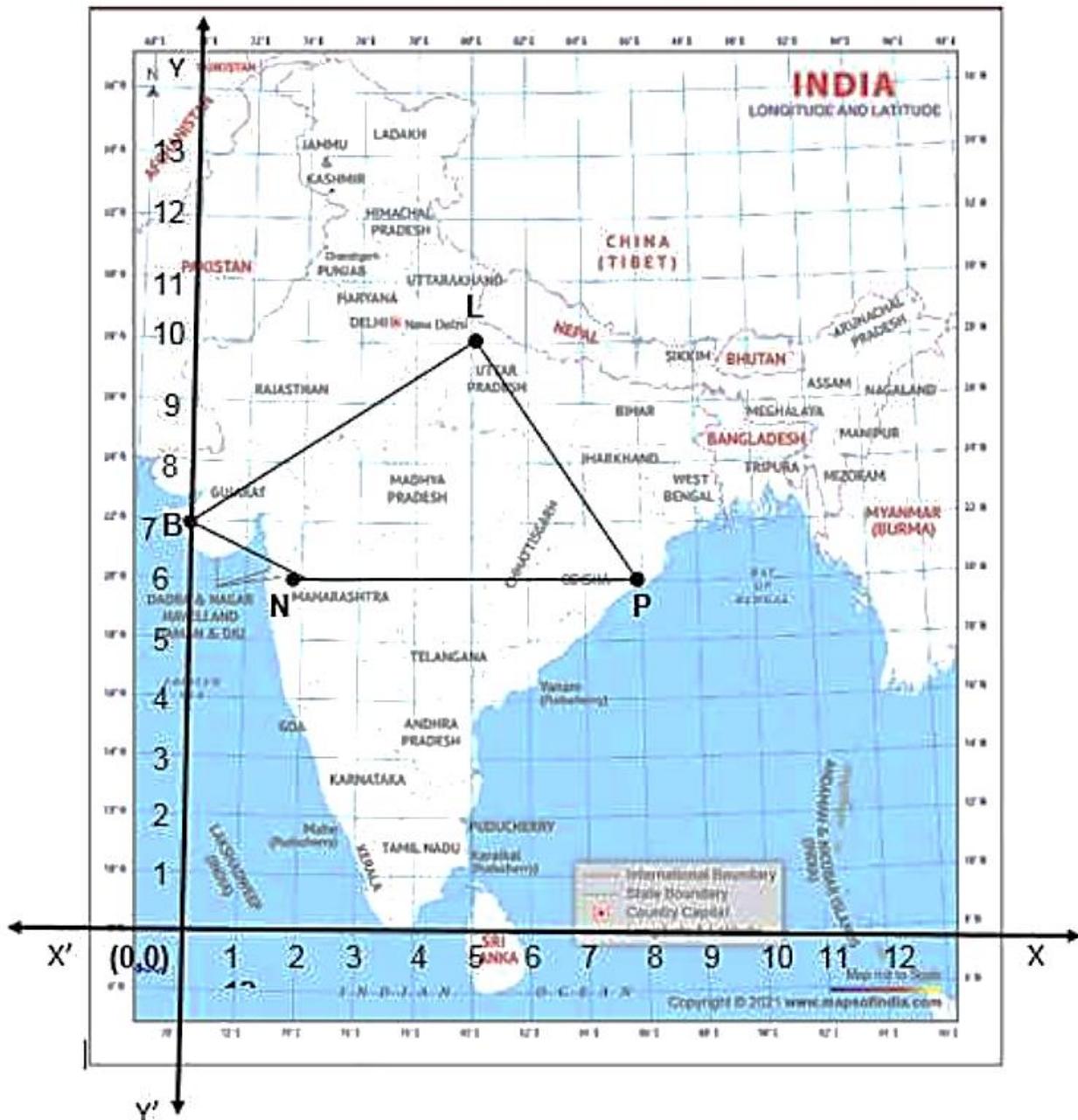
37. Case Study – 2:

In a GPS, The lines that run east-west are known as lines of latitude, and the lines running north-south are known as lines of longitude. The latitude and the longitude of a place are its coordinates and the distance formula is used to find the distance between two places. The distance between two parallel lines is approximately 150 km. A family from Uttar Pradesh planned a round trip from Lucknow (L) to Puri (P) via Bhuj (B) and Nashik (N) as shown in the given figure below.

- 1) Find the distance between Lucknow (L) to Bhuj(B).
- 2) If Kota (K), internally divide the line segment joining Lucknow (L) to Bhuj (B) into 3 : 2 then find the coordinate of Kota (K).
- 3) Name the type of triangle formed by the places Lucknow (L), Nashik (N) and Puri (P)

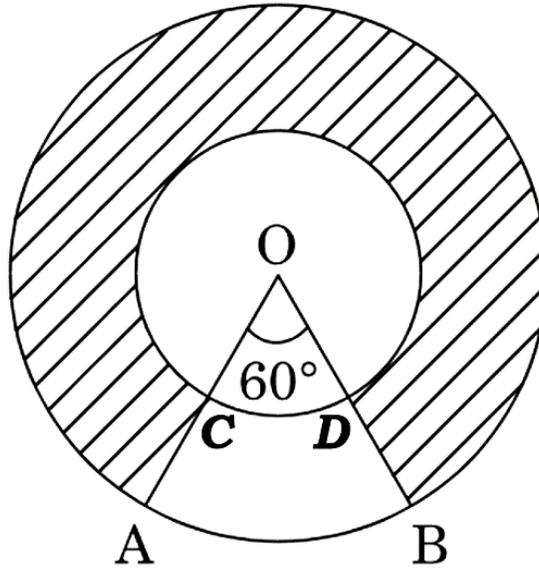
[OR]

Find a place (point) on the longitude (y-axis) which is equidistant from the points Lucknow (L) and Puri (P).



38. Case Study – 3:

Two concentric circles with centre O , have radii 21 cm and 42 cm. If $\angle AOB = 60^\circ$



- 1) Find Major Sector Area of OAB
- 2) Find Minor Sector Area of OCD
- 3) Find the shaded region

OR

Find the Area between $ABCD$