



Instructions

- Attempt all Questions.

1. Find the following integrals: (2)

$$\int (\sin x + \cos x) dx$$

2. Integrate $\frac{x^2}{1-x^6}$ (2)

3. Find the integral of $\frac{\cos x}{1 + \cos x}$ (2)

4. Evaluate the following integrals: (2)

$$\int_1^2 \frac{x dx}{(x+1)(x+2)}$$

5. Write an anti derivative for each of the following functions using the method of inspection: (2)

$$\cos^2 x$$

6. By using the properties of definite integrals, evaluate the integral: $\int_0^{\frac{\pi}{2}} \frac{\sqrt{\sin x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$ (2)

7. Integrate the following functions w.r.t. x: (2)

$$2x \sin(x^2 + 1)$$

8. $\int \sqrt{\frac{a+x}{a-x}}$ (2)

9. $\int_0^{\frac{\pi}{2}} \frac{dx}{(a^2 \cos^2 x + b^2 \sin^2 x)^2}$ (2)
(Hint: Divide Numerator and Denominator by $\cos^4 x$)

10. $\int_{-a}^a f(x) dx = 0$ if f is an _____ function. (2)

11. If $\int_0^a \frac{1}{1+4x^2} dx = \frac{\pi}{8}$, then $a =$ _____. (2)

12. Integrate $\frac{\sin x}{(1 + \cos x)^2}$ (2)

13. Integrate $\frac{5x - 2}{1 + 2x + 3x^2}$ (2)

14. Find an anti derivative (or integral) of the following functions by the method of inspection. e^{2x} (2)

15. By using the properties of definite integrals, evaluate $\int_0^2 \frac{6x + 3}{x^2 + 4} dx$ (2)

16. $\int \frac{\sin^6 x}{\cos^8 x} dx =$ _____. (2)

17. Find an anti derivative (or integral) of the following functions by the method of inspection. $\sin 2x$ (2)

18. Integrate $\frac{x^2}{(2 + 3x^3)^3}$ (2)

19. Find $\int x^2 \tan^{-1} x dx$ (2)
20. Find $\int_0^{\frac{\pi}{4}} \sqrt{1 + \sin 2x} dx$ (2)
21. Evaluate the integrals using substitution. $\int_{-1}^1 \frac{dx}{x^2 + 2x + 5}$ (2)
22. Find $\int_2^8 \frac{\sqrt{10-x}}{\sqrt{x} + \sqrt{10-x}} dx$ (2)
23. $\int_0^{\frac{\pi}{2}} \frac{\sin^n x dx}{\sin^n x + \cos^n x} = \text{_____}$. (2)
24. Integrate $\frac{1}{x^n - 1}$ (2)
25. Integrate $\frac{x}{(x^2 + 1)(x - 1)}$ (2)
26. Evaluate $\int_0^1 \frac{\tan^{-1} x}{1 + x^2} dx$ (2)
27. $\int \sqrt{2ax - x^2} dx$ (2)
28. The value of $\int_{-\pi}^{\pi} \sin^3 x \cos^2 x dx$ is _____. (2)
29. Integrate $\frac{x}{e^{x^2}}$ (2)
30. Find the integral of $\tan^3 2x \sec 2x$ (2)